

TAPM V4. Part 1: Technical Description.

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Abstract

Air pollution predictions for environmental impact assessments usually use Gaussian plume/puff models driven by observationally-based meteorological inputs. An alternative approach is to use prognostic meteorological and air pollution models, which have many advantages over the Gaussian approach and are now a viable tool for performing year-long simulations. This paper provides a comprehensive technical description of the newly enhanced prognostic model TAPM.

1 Introduction

Air pollution models that can be used to predict hour by hour pollution concentrations for periods of up to a year, are generally semi-empirical/analytic approaches based on Gaussian plumes or puffs. These models typically use either a simple surface based meteorological file or a diagnostic wind field model based on available observations. TAPM (The Air Pollution Model) is different to these approaches in that it solves approximations to the fundamental fluid dynamics and scalar transport equations to predict meteorology and pollutant concentration for a range of pollutants important for air pollution applications. TAPM consists of coupled prognostic meteorological and air pollution concentration components, eliminating the need to have site-specific meteorological observations. Instead, the model predicts the flows important to local-scale air pollution, such as sea breezes and terrain-induced flows, against a background of larger-scale meteorology provided by synoptic analyses.

The meteorological component of TAPM is an incompressible, non-hydrostatic, primitive equation model with a terrain-following vertical coordinate for three-dimensional simulations. The model solves the momentum equations for horizontal wind components, the incompressible continuity equation for vertical velocity, and scalar equations for potential virtual temperature and specific humidity of water vapour, cloud water/ice, rain water and snow. The Exner pressure function is split into hydrostatic and non-hydrostatic components, and a Poisson equation is solved for the non-hydrostatic component. Explicit cloud microphysical processes are included. The turbulence terms in these equations have been determined by solving equations for turbulence kinetic energy and eddy dissipation rate, and then using these values to represent vertical fluxes by a gradient diffusion approach, including counter-gradient terms. A vegetative canopy, soil scheme, and urban scheme are used at the surface, while radiative fluxes, both at the surface and at upper levels, are also included.

The air pollution component of TAPM, which uses the predicted meteorology and turbulence from the meteorological component, consists of four modules. The Eulerian Grid Module (EGM) solves prognostic equations for the mean and variance of concentration. The Lagrangian Particle Module (LPM) can be used to represent near-source dispersion more accurately. The Plume Rise Module is used to account for plume momentum and buoyancy effects for point sources. The Building Wake Module allows plume rise and dispersion to include wake effects on meteorology and turbulence. The model also includes gas-phase photochemical reactions based on the Generic Reaction Set, gas- and aqueous-phase chemical reactions for sulfur dioxide and particles, and a dust mode for total suspended particles (PM_{2.5}, PM₁₀, PM₂₀ and PM₃₀). Wet and dry deposition effects are also included.

This paper describes the technical details of the modelling approach, including the meteorological component in Section 2 and the pollution component in Section 3. Section 4 outlines the numerical methods used in the model. Part 2 of this paper (Hurley et al., 2008) presents a summary of some verification studies performed with TAPM V4.

2 Meteorological component

The meteorological component of TAPM is an incompressible, optionally non-hydrostatic, primitive equation model with a terrain-following vertical coordinate for three-dimensional simulations. It includes parameterisations for cloud/rain/snow micro-physical processes, turbulence closure, urban/vegetative canopy and soil, and radiative fluxes. The model solution for winds, potential virtual temperature and specific humidity, is weakly nudged with a 24-hour e-folding time towards the synoptic-scale input values of these variables.

Note that the horizontal model domain size is restricted in size to less than 1500 km x 1500 km, as the model equations neglect time zones, the curvature of the earth and assume a uniform distance grid spacing across the domain.

2.1 Base meteorological variables

The mean wind is determined for the horizontal components u and v (m s⁻¹) from the momentum equations and the terrain following vertical velocity $\dot{\sigma}$ (m s⁻¹) from the continuity equation. Potential virtual temperature θ_v (K) is determined from an equation combining conservation of heat and water vapour. The Exner pressure function $\pi = \pi_H + \pi_N$ (J kg⁻¹ K⁻¹) is determined from the sum of the hydrostatic component π_H and non-hydrostatic component π_N (see Section 2.2). The equations for these variables are as follows

$$\frac{du}{dt} = \frac{\partial}{\partial x} \left(K_H \frac{\partial u}{\partial x} \right) + \frac{\partial}{\partial y} \left(K_H \frac{\partial u}{\partial y} \right) - \frac{\partial \overline{w'u'}}{\partial \sigma} \frac{\partial \sigma}{\partial z} - \theta_v \left(\frac{\partial \pi}{\partial x} + \frac{\partial \pi}{\partial \sigma} \frac{\partial \sigma}{\partial x} \right) + fv + F(u) - N_s(u - u_s)$$
(1)

$$\frac{dv}{dt} = \frac{\partial}{\partial x} \left(K_H \frac{\partial v}{\partial x} \right) + \frac{\partial}{\partial y} \left(K_H \frac{\partial v}{\partial y} \right) - \frac{\partial \overline{w'v'}}{\partial \sigma} \frac{\partial \sigma}{\partial z} - \theta_v \left(\frac{\partial \pi}{\partial y} + \frac{\partial \pi}{\partial \sigma} \frac{\partial \sigma}{\partial y} \right) - fu + F(v) - N_s(v - v_s)$$
(2)

$$\frac{\partial \dot{\sigma}}{\partial \sigma} = -\left(\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y}\right) + u \frac{\partial}{\partial \sigma} \left(\frac{\partial \sigma}{\partial x}\right) + v \frac{\partial}{\partial \sigma} \left(\frac{\partial \sigma}{\partial y}\right)$$
(3)

$$\frac{d\theta_{v}}{dt} = \frac{\partial}{\partial x} \left(K_{H} \frac{\partial \theta_{v}}{\partial x} \right) + \frac{\partial}{\partial y} \left(K_{H} \frac{\partial \theta_{v}}{\partial y} \right) - \frac{\partial w' \theta_{v}'}{\partial \sigma} \frac{\partial \sigma}{\partial z} + S_{\theta_{v}} + F(\theta_{v}) - N_{s}(\theta_{v} - \theta_{vs})$$

$$\tag{4}$$

$$\frac{\partial \pi_H}{\partial \sigma} = -\frac{g}{\theta} \left(\frac{\partial \sigma}{\partial z} \right)^{-1} \tag{5}$$

where

t = time(s),

 $x, y, \sigma =$ the components of the coordinate system (m),

$$\sigma = z_T \left(\frac{z - z_s}{z_T - z_s} \right),$$

z =cartesian vertical coordinate (m),

 z_T = height of model top (m),

 $z_s = \text{terrain height (m)},$

$$\frac{d\phi}{dt} \equiv \frac{\partial \phi}{\partial t} + u \frac{\partial \phi}{\partial x} + v \frac{\partial \phi}{\partial y} + \dot{\sigma} \frac{\partial \phi}{\partial \sigma},$$

 K_H = horizontal diffusion coefficient (see Section 2.4),

 $\overline{w'\phi'}$ = vertical flux of ϕ (see Section 2.4),

 $F(\phi)$ = horizontal filtering of ϕ (see Section 4.3),

 $f = \text{Coriolis parameter} \left(4\pi_c \sin(lat)/(24 \times 3600)\right) (s^{-1}),$

 $\pi_c = 3.14159265,$

 $lat = latitude (^{\circ}),$

 u_s, v_s, θ_{vs} = large scale synoptic winds and potential virtual temperature,

 N_s = large scale nudging coefficient (1/(24×3600)),

$$S_{\theta_v} = \frac{\theta_v}{T} \left(\frac{\partial T}{\partial t} \right)_{RADIATION} - \frac{\lambda}{c_n} S_{q_v}$$
 (see Sections 2.3 and 2.5),

T = temperature (K),

 $g = \text{gravitational constant } (9.81 \,\text{m s}^{-2}),$

 λ = latent heat of vaporisation of water (2.5×10⁶ J kg⁻¹),

 c_p = specific heat at constant pressure (1006 J kg⁻¹ K⁻¹),

$$\frac{\partial \sigma}{\partial x} = \left(\frac{\sigma - z_T}{z_T - z_s}\right) \frac{\partial z_s}{\partial x}, \quad \frac{\partial \sigma}{\partial y} = \left(\frac{\sigma - z_T}{z_T - z_s}\right) \frac{\partial z_s}{\partial y}, \quad \frac{\partial \sigma}{\partial z} = \left(\frac{z_T}{z_T - z_s}\right).$$

2.2 Non-hydrostatic pressure

The optional non-hydrostatic component of the Exner pressure function π_N is determined by taking spatial derivatives of the three momentum equations and the time derivative of the continuity equation, and then eliminating all time derivatives in the continuity equation by substitution. The following assumes all products of Coriolis terms and terrain gradients, and all turbulence and synoptic variation terms, can be neglected. The resultant equation for π_N is

$$\frac{\partial^{2} \pi_{N}}{\partial x^{2}} + 2 \frac{\partial \sigma}{\partial x} \frac{\partial^{2} \pi_{N}}{\partial x \partial \sigma} + \frac{\partial^{2} \pi_{N}}{\partial y^{2}} + 2 \frac{\partial \sigma}{\partial y} \frac{\partial^{2} \pi_{N}}{\partial y \partial \sigma} + \left(\frac{\partial \sigma}{\partial z}\right)^{2} \frac{\partial^{2} \pi_{N}}{\partial \sigma^{2}} + C_{x} \frac{\partial \pi_{N}}{\partial x} + C_{y} \frac{\partial \pi_{N}}{\partial y} + C_{\sigma} \frac{\partial \pi_{N}}{\partial \sigma} = R_{\pi},$$
(6)

with coefficients

$$\begin{split} &C_{x} = \frac{1}{\theta_{v}} \left(\frac{\partial \theta_{v}}{\partial x} + \frac{\partial \theta_{v}}{\partial \sigma} \frac{\partial \sigma}{\partial x} \right), \ C_{y} = \frac{1}{\theta_{v}} \left(\frac{\partial \theta_{v}}{\partial y} + \frac{\partial \theta_{v}}{\partial \sigma} \frac{\partial \sigma}{\partial y} \right), \\ &C_{\sigma} = \frac{1}{\theta_{v}} \left(\frac{\partial \theta_{v}}{\partial x} \frac{\partial \sigma}{\partial x} + \frac{\partial \theta_{v}}{\partial y} \frac{\partial \sigma}{\partial y} + \frac{\partial \theta_{v}}{\partial \sigma} \left(\frac{\partial \sigma}{\partial z} \right)^{2} \right) + \frac{\partial^{2} \sigma}{\partial x^{2}} + \frac{\partial^{2} \sigma}{\partial y^{2}}, \\ &R_{\pi} = \frac{1}{\theta_{v}} \left(\frac{\partial R_{u}}{\partial x} + \frac{\partial R_{v}}{\partial y} + \frac{\partial R_{\sigma}}{\partial \sigma} - R_{u} \frac{\partial}{\partial \sigma} \left(\frac{\partial \sigma}{\partial x} \right) - R_{v} \frac{\partial}{\partial \sigma} \left(\frac{\partial \sigma}{\partial y} \right) \right), \end{split}$$

$$\begin{split} R_{u} &= -u \, \frac{\partial u}{\partial x} - v \, \frac{\partial u}{\partial y} - \dot{\sigma} \, \frac{\partial u}{\partial \sigma} + f v - \theta_{v} \, \frac{\partial \pi_{H}}{\partial x} + g \, \frac{\partial \sigma}{\partial x} \left(\frac{\partial \sigma}{\partial z} \right)^{-1}, \\ R_{v} &= -u \, \frac{\partial v}{\partial x} - v \, \frac{\partial v}{\partial y} - \dot{\sigma} \, \frac{\partial v}{\partial \sigma} - f u - \theta_{v} \, \frac{\partial \pi_{H}}{\partial y} + g \, \frac{\partial \sigma}{\partial y} \left(\frac{\partial \sigma}{\partial z} \right)^{-1}, \\ R_{\dot{\sigma}} &= -u \, \frac{\partial \dot{\sigma}}{\partial x} - v \, \frac{\partial \dot{\sigma}}{\partial y} - \dot{\sigma} \, \frac{\partial \dot{\sigma}}{\partial \sigma} - \theta_{v} \left(\frac{\partial \pi_{H}}{\partial x} \, \frac{\partial \sigma}{\partial x} + \frac{\partial \pi_{H}}{\partial y} \, \frac{\partial \sigma}{\partial y} \right) \\ &+ u^{2} \, \frac{\partial^{2} \sigma}{\partial x^{2}} + 2uv \, \frac{\partial^{2} \sigma}{\partial x \partial y} + v^{2} \, \frac{\partial^{2} \sigma}{\partial y^{2}} + 2\dot{\sigma} \left(u \, \frac{\partial}{\partial \sigma} \left(\frac{\partial \sigma}{\partial x} \right) + v \, \frac{\partial}{\partial \sigma} \left(\frac{\partial \sigma}{\partial y} \right) \right), \end{split}$$

and

$$\frac{\partial}{\partial \sigma} \left(\frac{\partial \sigma}{\partial x} \right) = \left(\frac{1}{z_T - z_s} \right) \frac{\partial z_s}{\partial x}, \quad \frac{\partial}{\partial \sigma} \left(\frac{\partial \sigma}{\partial y} \right) = \left(\frac{1}{z_T - z_s} \right) \frac{\partial z_s}{\partial y},$$

$$\frac{\partial^2 \sigma}{\partial x^2} = \left(\frac{\sigma - z_T}{z_T - z_s} \right) \frac{\partial^2 z_s}{\partial x^2}, \quad \frac{\partial^2 \sigma}{\partial x \partial y} = \left(\frac{\sigma - z_T}{z_T - z_s} \right) \frac{\partial^2 z_s}{\partial x \partial y}, \quad \frac{\partial^2 \sigma}{\partial y^2} = \left(\frac{\sigma - z_T}{z_T - z_s} \right) \frac{\partial^2 z_s}{\partial y^2}.$$

2.3 Water and ice micro-physics

Conservation equations are solved for specific humidity (kg kg⁻¹) $q = q_V + q_C + q_I$ (representing the sum of water vapour, cloud water and cloud ice respectively), specific humidity (kg kg⁻¹) of rain water q_R and specific humidity (kg kg⁻¹) of snow q_S :

$$\frac{dq}{dt} = \frac{\partial}{\partial x} \left(K_H \frac{\partial q}{\partial x} \right) + \frac{\partial}{\partial y} \left(K_H \frac{\partial q}{\partial y} \right) - \frac{\partial \overline{w'q'}}{\partial \sigma} \frac{\partial \sigma}{\partial z} + S_{q_v} + S_{q_c} + S_{q_l} - N_{syn} \left(q - q_{syn} \right)$$
(7)

$$\frac{dq_R}{dt} = \frac{\partial}{\partial x} \left(K_H \frac{\partial q_R}{\partial x} \right) + \frac{\partial}{\partial v} \left(K_H \frac{\partial q_R}{\partial v} \right) - \frac{\partial \overline{w'q'_R}}{\partial \sigma} \frac{\partial \sigma}{\partial z} + S_{q_R} - V_{TR} \frac{\partial q_R}{\partial \sigma} \frac{\partial \sigma}{\partial z}$$
(8)

$$\frac{dq_{s}}{dt} = \frac{\partial}{\partial x} \left(K_{H} \frac{\partial q_{s}}{\partial x} \right) + \frac{\partial}{\partial y} \left(K_{H} \frac{\partial q_{s}}{\partial y} \right) - \frac{\partial \overline{w'q'_{s}}}{\partial \sigma} \frac{\partial \sigma}{\partial z} + S_{q_{s}} - V_{TS} \frac{\partial q_{s}}{\partial \sigma} \frac{\partial \sigma}{\partial z}$$
(9)

with

 $S_{q_{V}}$, $S_{q_{C}}$, $S_{q_{I}}$, $S_{q_{R}}$, $S_{q_{S}}=$ micro - physical source terms,

 q_{syn} = synoptic scale specific humidity of water vapour plus cloud water/ice,

 V_{TR} , V_{TS} = terminal velocity of rain/snow,

and the specific humidity of water vapour $q_{\scriptscriptstyle V}$ and the saturated specific humidity $q_{\scriptscriptstyle VS}$ determined from

$$q_V = \min(q, q_{VS}),$$

 $q_{VS} = \frac{0.622e_{VS}}{(p - 0.378e_{VS})},$

p = pressure (Pa), and

$$e_{VS} = 610 \exp\left(\frac{\lambda}{R_{v}} \left(\frac{1}{273.15} - \frac{1}{T}\right)\right),$$

$$\lambda = \begin{cases} L_{v}, & \text{if } T \ge 273.15 \\ L_{s}, & \text{if } T < 273.15 \end{cases}$$

Cloud water and cloud ice are assumed to co-exist only between temperatures of -15°C and 0°C, with a linear relationship used between these two limits (see Rotstayn (1997) for a discussion of mixed-phase clouds):

$$q_C = \left(1 + \left(\frac{T - 273.15}{15}\right)\right)(q - q_V),$$

$$q_I = q - q_V - q_C.$$

The source terms in the conservation equations are

$$\begin{split} S_{q_{V}} &= -P_{VC} - P_{VI} - P_{VR} - P_{VS} \,, \\ S_{q_{C}} &= P_{VC} - P_{CI} - P_{CR} - P_{CS} \,, \\ S_{q_{I}} &= P_{VI} + P_{CI} - P_{IR} - P_{IS} \,, \\ S_{q_{R}} &= P_{VR} + P_{CR} + P_{IR} - P_{RS} \,, \\ S_{q_{S}} &= P_{VS} + P_{CS} + P_{IS} + P_{RS} \,. \end{split}$$

Bulk parameterisations of the micro-physics are based mainly on Tripoli and Cotton (1980) and Lin et al. (1983), with some updated constants/parameterisations as used by Katzfey and Ryan (1997), Rotstayn (1997) and Ryan (2002). The micro-physical production terms used here are as follows:

$$\begin{split} P_{VC} &= \left(\frac{q_V - q_{VS}}{\Delta t}\right) \left(1 + \frac{L_V}{c_p} \frac{dq_{VS}}{dT}\right)^{-1} \\ P_{VI} &= \left(\frac{q_V - q_{VS}}{\Delta t}\right) \left(1 + \frac{L_S}{c_p} \frac{dq_{VS}}{dT}\right)^{-1} \\ P_{CI} &= 0 \end{split}$$

$$P_{IR}=0$$

$$P_{CR} = P_{CR1} + P_{CR2}$$

$$P_{CR1} = \frac{0.104 E_{CR1} g}{\mu} H(q_C - q_{C0}) \left(\frac{\rho^4 q_C^7}{N_C \rho_W}\right)^{1/3}$$

$$P_{CR2} = \frac{\pi}{4} E_{CR2} a_R N_{R0} \Gamma(3.5) \left(\frac{\rho}{\rho_0}\right)^{1/2} q_C \lambda_R^{-3.5}$$

$$P_{CS} = \frac{\pi}{4} E_{CS} a_S N_{S0} \Gamma(3.25) \left(\frac{\rho}{\rho_0}\right)^{1/2} q_C \lambda_S^{-3.25}$$

$$\begin{split} P_{IS} &= P_{IS1} + P_{IS2} \\ P_{IS1} &= 0.005 E_{IS} (q_I - q_{I0}) H (q_I - q_{I0}) \\ P_{IS2} &= \frac{\pi}{4} E_{IS} a_S N_{S0} \Gamma(3.25) \left(\frac{\rho}{\rho_0}\right)^{1/2} q_I \lambda_S^{-3.25} \end{split}$$

$$P_{VR} = \min(0, \frac{q_V}{q_{VS}} - 1) \frac{q_R \lambda_R^2}{\rho_W} \left(\frac{0.5 + \frac{0.349}{\mu^{1/2}} \left(\frac{\rho_W g \rho}{\lambda_R^3} \right)^{1/4}}{\frac{L_V^2}{K R_V T^2} + \frac{R_V T}{e_{VS} D_V}} \right)$$

$$P_{VS} = \frac{2\pi}{\rho} \min(0, \frac{q_V}{q_{VS}} - 1) \left(\frac{\frac{0.78}{\lambda_S^2} + \frac{0.31\Gamma(2.625)a_S^{1/2}\left(\frac{\rho_0}{\rho}\right)^{1/4}}{v^{1/2}\lambda_S^{2.625}} \left(\frac{\rho_0}{\rho}\right)^{1/4}}{\frac{L_S^2}{KR_V T^2} + \frac{R_V T}{e_{VS}D_V}} \right)$$

$$P_{RS} = -q_S / \Delta t$$
 if $T > 275.15$.

where H is the Heaviside function,

$$\begin{split} \lambda_R &= \left(\frac{\pi \rho_R N_{R0}}{\rho q_R}\right)^{1/4}, \ \lambda_S = \left(\frac{\pi \rho_S N_{S0}}{\rho q_S}\right)^{1/4}, \\ a_R &= 141.5, \ a_S = 4.84, \\ q_{C0} &= \frac{4}{3} \pi \rho_W r_C^3 N_C \rho^{-1}, \\ q_{CI} &= \begin{cases} \rho 2.316 \times 10^{(-6.0 - 0.0413(T - 273.15))}, \ \text{if } T > 255.65, \\ \rho 1.158 \times 10^{(-4.0 + 0.0519(T - 273.15))}, \ \text{otherwise} \end{cases}, \\ E_{CR1} &= 0.55, \ E_{CR2} = 0.7, \ E_{CS} = 0.7, \ E_{IS} = \exp(0.025(T - 273.15)). \end{split}$$

Other constants are

$$\begin{split} L_V &= 2.5 \times 10^6 \text{ J kg}^{\text{-1}}, L_S = 2.83 \times 10^6 \text{ J kg}^{\text{-1}}, \\ N_C &= 3 \times 10^8 \text{ m}^{\text{-3}}, \text{r}_{C0} = 1 \times 10^{\text{-5}} \text{ m}, N_{R0} = 8 \times 10^6 \text{ m}^{\text{-4}}, N_{S0} = 3 \times 10^6 \text{ m}^{\text{-4}}, \\ \rho_W &= 1000 \text{ kg m}^{\text{-3}}, \rho_S = 100 \text{ kg m}^{\text{-3}}, R_V = 461.5 \text{ J kg}^{\text{-1}} \text{ K}^{\text{-1}}, \\ \mu &= 1.8 \times 10^{\text{-5}} \text{ kg m}^{\text{-1}} \text{ s}^{\text{-1}}, \nu = 1.35 \times 10^{\text{-5}} \text{ m}^2 \text{ s}^{\text{-1}}, \\ K &= 0.025 \text{ J m}^{\text{-1}} \text{ s}^{\text{-1}}, D_V = 2.5 \times 10^{\text{-5}} \text{ m}^2 \text{ s}^{\text{-1}}. \end{split}$$

The rain/snow terminal velocity is determined from

$$\begin{split} V_{TR} &= -\frac{a_R \Gamma(4.5)}{6 \lambda_R^{0.5}} \left(\frac{\rho_0}{\rho} \right)^{1/2}, \\ V_{TS} &= -\frac{a_S \Gamma(4.25)}{6 \lambda_S^{0.25}} \left(\frac{\rho_0}{\rho} \right)^{1/2}. \end{split}$$

Calculation of the precipitation rate (m s⁻¹) at the surface is from $P = \frac{\rho}{\rho_W} V_{TR} q_R(0)$, where $q_R(0)$ is the amount of rain reaching the ground, and similarly for snowfall, but using snow density, terminal velocity and specific humidity.

2.4 Turbulence and diffusion

Turbulence closure in the mean prognostic equations uses a gradient diffusion approach with non-local or counter-gradient corrections, which depends on a diffusion coefficient K and gradients of mean variables and a mass-flux approach based on Soares et al. (2004) and Hurley (2007). The vertical fluxes are parameterised as follows:

$$\overline{w'u'} = -K \left(\frac{\partial u}{\partial \sigma} \frac{\partial \sigma}{\partial z} - \gamma_u \right) \equiv -K \frac{\partial u}{\partial \sigma} \frac{\partial \sigma}{\partial z} + MU, \tag{10}$$

$$\overline{w'v'} = -K \left(\frac{\partial v}{\partial \sigma} \frac{\partial \sigma}{\partial z} - \gamma_v \right) \equiv -K \frac{\partial v}{\partial \sigma} \frac{\partial \sigma}{\partial z} + MV, \tag{11}$$

$$\overline{w'\theta_{v}'} = -K \left(\frac{\partial \theta_{v}}{\partial \sigma} \frac{\partial \sigma}{\partial z} - \gamma_{\theta} \right) \equiv -K \frac{\partial \theta_{v}}{\partial \sigma} \frac{\partial \sigma}{\partial z} + M \left(\theta_{v},_{up} - \theta_{v} \right), \tag{12}$$

$$\overline{w'\phi'} = -2.5K \frac{\partial \phi}{\partial \sigma} \frac{\partial \sigma}{\partial z} \tag{13}$$

where ϕ is a general scalar variable, K is the eddy diffusivity and γ_u , γ_v and γ_θ are the non-local fluxes. Horizontal fluxes are parameterised using a gradient diffusion approach. The scalar diffusion coefficient of 2.5 used above is based on an analysis of the second order closure equations from Andren (1990), with constants from Rodi (1985).

The turbulence scheme used to calculate K is the standard E- ε model in three-dimensional terrain-following coordinates, with constants for the eddy dissipation rate equation derived from the analysis of Duynkerke (1988). The model solves prognostic equations for the turbulence kinetic energy (E) and the eddy dissipation rate (ε)

$$\frac{dE}{dt} = \frac{\partial}{\partial x} \left(K_H \frac{\partial E}{\partial x} \right) + \frac{\partial}{\partial y} \left(K_H \frac{\partial E}{\partial y} \right) + \left(\frac{\partial \sigma}{\partial z} \right)^2 \frac{\partial}{\partial \sigma} \left(K \frac{\partial E}{\partial \sigma} \right) + P_s + P_b - \varepsilon, \tag{14}$$

$$\frac{d\varepsilon}{dt} = \frac{\partial}{\partial x} \left(K_H \frac{\partial \varepsilon}{\partial x} \right) + \frac{\partial}{\partial y} \left(K_H \frac{\partial \varepsilon}{\partial y} \right) + \left(\frac{\partial \sigma}{\partial z} \right)^2 \frac{\partial}{\partial \sigma} \left(c_{\varepsilon 0} K \frac{\partial \varepsilon}{\partial \sigma} \right)$$

$$+\frac{\mathcal{E}}{E}\left(c_{\varepsilon 1}\left(\max(0, P_t) + P_s + \max(0, P_b)\right) - c_{\varepsilon 2}\varepsilon\right),\tag{15}$$

where

$$\begin{split} P_t &= \begin{cases} \left(\frac{\partial \sigma}{\partial z}\right)^2 \frac{\partial}{\partial \sigma} \left(K \frac{\partial E}{\partial \sigma}\right), \text{ if } \theta_{v^*} < 0 \\ 0, \text{ otherwise} \end{cases} \\ P_s &= 2K \left(\left(\frac{\partial u}{\partial x} + \frac{\partial u}{\partial \sigma} \frac{\partial \sigma}{\partial x}\right)^2 + \left(\frac{\partial v}{\partial y} + \frac{\partial v}{\partial \sigma} \frac{\partial \sigma}{\partial y}\right)^2 + \left(\frac{\partial w}{\partial \sigma} \frac{\partial \sigma}{\partial z}\right)^2 \right) \\ &+ K \left(\left(\frac{\partial u}{\partial y} + \frac{\partial u}{\partial \sigma} \frac{\partial \sigma}{\partial y} + \frac{\partial v}{\partial x} + \frac{\partial v}{\partial \sigma} \frac{\partial \sigma}{\partial x}\right)^2 \right) \\ &+ K \left(\left(\frac{\partial u}{\partial \sigma} \frac{\partial \sigma}{\partial z} + \frac{\partial w}{\partial x} + \frac{\partial w}{\partial \sigma} \frac{\partial \sigma}{\partial x}\right)^2 + \left(\frac{\partial v}{\partial \sigma} \frac{\partial \sigma}{\partial z} + \frac{\partial w}{\partial y} + \frac{\partial w}{\partial \sigma} \frac{\partial \sigma}{\partial y}\right)^2 \right) \\ &- K \left(\gamma_u \left(\frac{\partial u}{\partial \sigma} \frac{\partial \sigma}{\partial z} + \frac{\partial w}{\partial x} + \frac{\partial w}{\partial \sigma} \frac{\partial \sigma}{\partial x}\right) + \gamma_v \left(\frac{\partial v}{\partial \sigma} \frac{\partial \sigma}{\partial z} + \frac{\partial w}{\partial y} + \frac{\partial w}{\partial \sigma} \frac{\partial \sigma}{\partial y}\right) \right), \\ P_b &= -\frac{g}{\theta_v} K \left(\frac{\partial \theta_v}{\partial \sigma} \frac{\partial \sigma}{\partial z} - \gamma_\theta\right), \\ \text{with } w &= \left(\frac{\partial \sigma}{\partial z}\right)^{-1} \left(\dot{\sigma} - u \frac{\partial \sigma}{\partial x} - v \frac{\partial \sigma}{\partial y}\right), \end{split}$$

and
$$K_H = \max(10, K)$$
, $K = c_m \frac{E^2}{\epsilon}$, $c_m = 0.09$, $c_{\epsilon 0} = 0.69$, $c_{\epsilon 1} = 1.46$, and $c_{\epsilon 2} = 1.83$.

Turbulence kinetic energy and eddy dissipation rate are enhanced in the top-half of the convective boundary layer (CBL), where turbulence levels can be underestimated using the above approaches. This has been achieved by using a simple parameterisation that limits the rate of decrease of prognostic turbulence with height, between heights in the range 0.55-0.95 times the CBL height, provided that the height is above the surface layer and the convective velocity scale is greater than 0.5 m s^{-1} .

Vertical velocity variance $\overline{w'^2}$ is diagnosed from the following modified prognostic equation of Gibson and Launder (1978) and Andren (1990), when all advection and diffusion terms are neglected and the boundary-layer assumption is made (see Mellor and Yamada, 1982),

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$$\overline{w'^{2}} = \left(\frac{2}{3}E + \frac{E}{c_{s1}\varepsilon}\left((2 - c_{s2} - c_{w2}\frac{l}{kz})P_{s} + (2 - c_{s3} - c_{w3}\frac{l}{kz})P_{b} - \frac{2}{3}\varepsilon\right)\right) \cdot \left(1 + \frac{c_{w1}}{c_{s1}}\frac{l}{kz}\right)^{-1},$$

with constants from Rodi (1985)

$$c_{s1} = 2.20, c_{s2} = 1.63, c_{s3} = 0.73, c_{w1} = 1.00, c_{w2} = 0.24, c_{w3} = 0.0$$

The U and V terms in the non-local vertical momentum fluxes are

$$U=\frac{\overline{w'u'}}{E^{1/2}}\bigg|_{0},$$

$$V = \frac{\overline{w'v'}}{E^{1/2}}\bigg|_{0},$$

where subscript 0 denotes evaluation in the surface layer, which in practise means evaluation at the first model level using E, friction velocity and mean wind components. In order to aid numerical stability, particularly in the early-morning shallow CBL, the absolute values of γ_u and γ_v are kept below 0.001 s⁻¹.

In order to calculate the non-local vertical temperature flux, the virtual potential temperature (K) and specific humidity (kg kg⁻¹) in the convective updraft θ_v , $_{up}$ and q_{up} are obtained from

$$\frac{\partial \theta_{v},_{up}}{\partial z} = \varepsilon_{E} (\theta_{v},_{up} - \theta_{v}),$$

$$\frac{\partial q_{up}}{\partial z} = \varepsilon_E (q_{up} - q),$$

with boundary conditions θ_{v} , $_{up} = \theta_{v} + \frac{\overline{w'\theta'_{v}}}{E^{1/2}}\Big|_{0}$ and $q_{up} = q + \frac{\overline{w'q'}}{E^{1/2}}\Big|_{0}$ at the first model level.

Then, when the specific humidity in an updraft is greater than the saturated value $(q_{up} < q_{up,sat})$, the mass-flux M (m s⁻¹) is determined from

$$M = a_{up} W_{up}$$

or otherwise from

$$\frac{1}{M}\frac{\partial M}{\partial \sigma}\frac{\partial \sigma}{\partial z} = \varepsilon_{ent} - \delta_{ent},$$

with constants $a_{up} = 0.1$, $\varepsilon_{ent} = 2 \times 10^{-3}$ and $\delta_{ent} = 3 \times 10^{-3}$, and boundary condition for M at the level of saturation $M = a_C a_{up} w_{up}$, where $a_C = 0.5 + \arctan\left(1.55(q_{up} - q_{up,sat})/\sigma_{qup}\right)$ from

Cuijpers and Bechtold (1995) and
$$\sigma_{qup}^2 = \max \left(1 \times 10^{-6}, -1.6 \frac{E}{\varepsilon} \overline{w' q'_{up}} \frac{\partial q_{up}}{\partial \sigma} \frac{\partial \sigma}{\partial z} \right)$$
 from a

simplified second order closure equation based on Andren (1990). Note that M is set to zero when w_{up} is zero.

The vertical velocity in the convective updraft w_{up} is obtained from

$$\frac{1}{2}\frac{\partial w_{up}^2}{\partial z}\frac{\partial \sigma}{\partial z} = -\varepsilon_E b_1 w_{up}^2 + b_2 \frac{g}{\theta_v} (\theta_v, u_p - \theta_v),$$

with
$$b_1 = 1$$
, $b_2 = 2$, $\varepsilon_E = 0.5 \left(\frac{1}{z + \Delta z} + \frac{1}{\max(0, z_i - z) + \Delta z} \right)$, and $w_{up} = 0$ at the surface.

These equations are integrated with increasing height using an implicit solution method. In order to aid numerical stability, particularly in the early-morning shallow CBL, the value of γ_{θ} is kept within the range of zero and 0.002 K m⁻¹.

The boundary-layer height (z_i) in convective conditions is defined as the first model level above the surface for which the updraft velocity decreases to zero, while in stable/neutral conditions it is defined as the first model level above the surface that has a vertical heat flux less than 5% of the surface value following Derbyshire (1990).

The mass-flux approach used in the turbulence closure also allows the calculation of the contribution of the large convective eddies to the vertical velocity variance and the Lagrangian timescale, following the analyses of deRoode et al. (2000)

$$\left(\overline{w'^2}\right)_{MF} = 4M^2,$$

$$\left(T_{L}\right)_{MF}=\frac{1}{5M\varepsilon_{E}},$$

where the subscript MF refers to the mass-flux contribution (note that in the last equation we have assumed that detrainment is 1.5 times entrainment, consistent with the mass-flux approach). The eddy dissipation rate can then be calculated as

$$(\varepsilon)_{MF} = \frac{\left(\overline{w'^2}\right)_{MF}}{\left(T_L\right)_{ME}} = 20M^3 \varepsilon_E,$$

and consistent with the formulation of the eddy diffusivity from the previous section, the corresponding eddy diffusivity can be calculated using

$$(K)_{MF} = c_m \frac{\left(\frac{1}{2} \overline{w'^2}\right)_{MF}^2}{(\varepsilon)_{MF}} = \frac{c_m M}{5\varepsilon_E}.$$

The total vertical velocity variance, eddy dissipation rate and eddy diffusivity is then just the sum of the contributions from the gradient closure and the mass-flux contribution. Note that the use of the total diffusivity for a scalar would only be required if the turbulence closure for the scalar flux does not explicitly include a non-local flux term.

2.5 Radiation

2.5.1 Clear-sky

Radiation at the surface is used for the computation of surface boundary conditions and scaling variables (see later), with the clear-sky incoming short-wave component from Mahrer and Pielke (1977),

$$R_{sw(clear-sky)}^{in} = \begin{cases} (a_g - a_w(z_s))S_{\text{Slope}}S_o \cos \chi; \text{ for } \cos \chi > 0\\ 0; & \text{for } \cos \chi \leq 0 \end{cases}$$

and the clear-sky incoming long-wave component from Dilley and O'Brien (1999),

$$R_{lw(clear-sky)}^{in} = \left(59.38 + 113.7 \left(\frac{T(\sigma_1)}{273.15}\right)^6 + 96.96 \left(\frac{r(\sigma_1)}{25}\right)^{1/2}\right) \cos \alpha,$$

with

$$a_g = 0.485 + 0.515 (1.014 - 0.16 / \sqrt{\cos \chi}),$$

$$a_w(\sigma) = 0.039 \left(\frac{r(\sigma)}{\cos \chi}\right)^{0.3},$$

 $r(\sigma) = \int_{\sigma}^{z_T} \rho q d\sigma$ is the column water vapour amount (kg m⁻² or mm) between z_T and σ , χ is the zenith angle, and S_o is the solar constant (1367 W m⁻²).

The solar declination, zenith, and terrain slope angles are calculated using

$$\sin \delta_s = \sin(23.5\pi_c/180)\sin(2\pi_c day/365),$$

$$\cos \chi = \cos(lat)\cos \delta_s \cos(\pi_c(hour - 12)/12) + \sin(lat)\sin \delta_s$$

$$S_{\text{Slope}} = \frac{\cos i}{\cos \chi}, \quad \cos i = \cos \alpha_{Slope} \cos \chi + \sin \alpha_{Slope} \sin \chi \cos(\beta - \eta_{Slope}),$$

$$\alpha_{\text{Slope}} = \tan^{-1} \left(\left(\frac{\partial z_s}{\partial x} \right)^2 + \left(\frac{\partial z_s}{\partial y} \right)^2 \right), \quad \eta_{Slope} = \tan^{-1} \left(\left(\frac{\partial z_s}{\partial y} \right) \left(\frac{\partial z_s}{\partial x} \right)^{-1} \right) - \frac{\pi_c}{2},$$

$$\beta = \sin^{-1}(\cos \delta_s \sin(\pi_c(hour - 12)/12)/\sin \chi),$$

lat = latitude, day = day of year ($1 \equiv 21$ March),

 $hour = hour of day (24 hour clock), \pi_c = 3.14159265.$

The effects of water vapour and carbon dioxide on atmospheric heating/cooling rates for both short-wave and long-wave radiation follow Mahrer and Pielke (1977)

$$\begin{split} \frac{\partial T}{\partial t}\bigg|_{RADIATION(clear-sky)} &= \frac{1}{\rho c_p} \left(-S_o \cos \chi \frac{\partial a_w}{\partial \sigma} \frac{\partial \sigma}{\partial z} \right. \\ &\left. -\sigma_{SB} \frac{\partial \varepsilon \uparrow}{\partial \sigma} \frac{\partial \sigma}{\partial z} \left((T(\sigma))^4 - (T(0))^4 \right) - \sigma_{SB} \frac{\partial \varepsilon \downarrow}{\partial \sigma} \frac{\partial \sigma}{\partial z} \left((T(z_T))^4 - (T(\sigma))^4 \right) \right], \end{split}$$

with

$$a_{w}(\sigma) = 0.039 \left(\frac{r(\sigma)}{\cos \chi}\right)^{0.3},$$

$$r(\sigma) = \int_{\sigma}^{z_T} \rho q_{v} d\sigma,$$

and emissivity $\varepsilon = \varepsilon_{q_v} + \varepsilon_{CO_2}$ either integrated upwards $(\varepsilon \uparrow)$ or downwards $(\varepsilon \downarrow)$ with

$$\varepsilon_{q_{v}} = \begin{cases} 0.113\log_{10}\left(1+12.6\delta P\right), & \text{for } \log_{10}\delta P \leq -4 \\ 0.104\log_{10}\delta P+0.440, & \text{for } -4<\log_{10}\delta P \leq -3 \\ 0.121\log_{10}\delta P+0.491, & \text{for } -3<\log_{10}\delta P \leq -1.5 \\ 0.146\log_{10}\delta P+0.527, & \text{for } -1.5<\log_{10}\delta P \leq -1, \\ 0.161\log_{10}\delta P+0.542, & \text{for } -1<\log_{10}\delta P \leq 0 \\ 0.136\log_{10}\delta P+0.542, & \text{for } \log_{10}\delta P>0 \end{cases}$$

$$\varepsilon_{CO_{2}} = 0.185\left(1-\exp\left(-0.39\left(\delta H\right)^{0.4}\right)\right),$$

$$\delta P = 0.1r(\sigma) = \begin{cases} 0.1 \int_{z_{S}}^{\sigma} \rho q_{v} d\sigma, & \text{for } \varepsilon \uparrow \\ 0.1 \int_{\sigma}^{z_{T}} \rho q_{v} d\sigma, & \text{for } \varepsilon \downarrow \end{cases},$$

$$\delta H = \begin{cases} 0.252(p_{S} - p)/100, & \text{for } \varepsilon \uparrow \\ 0.252(p - p_{T})/100, & \text{for } \varepsilon \downarrow \end{cases},$$

$$\delta H = \begin{cases} 0.252(p_S - p)/100, & \text{for } \varepsilon \uparrow \\ 0.252(p - p_T)/100, & \text{for } \varepsilon \downarrow \end{cases}$$

p is pressure (hPa),

subscripts S and T indicate the ground surface or model top respectively,

and $\sigma_{SB} = 5.67 \times 10^8 \text{ W m}^{-2} \text{ K}^{-4}$ is the Stefan Boltzman constant.

2.5.2 Cloudy sky

The clear-sky incoming radiation components from the previous section are modified for liquid water effects using an approach based on Stephens (1978). The method assumes clear and cloudy sky contributions can be treated separately.

The incoming short-wave radiation is

$$R_{sw}^{in}(\sigma) = R_{sw(clear-skv)}^{in} \Psi_{Transmission}$$

and using a fit to within 0.05 of the Ψ functions from Figure 3 of Stephens (1978) for transmission/absorption of short-wave radiation (ignoring zenith angle dependence)

$$\Psi_{Transmission} = \begin{cases} \exp(-16W^{in} + 13W^{in^2}), & W^{in} \le 0.11, \\ 0.2; & W^{in} > 0.11, \end{cases}$$

$$\Psi_{Absorption} = \begin{cases} 0.3W^{in^{1/2}}; & W^{in} \leq 0.11 \\ 0.1; & W^{in} > 0.11 \end{cases}.$$

The incoming long-wave radiation is

$$R_{lw}^{in}(\sigma) = R_{lw(clear-sky)}^{in} \left(1 - \varepsilon_{lw}^{in}(\sigma) \right) + \varepsilon_{lw}^{in}(\sigma) \sigma_{SB} T^{4}(\sigma),$$

$$\varepsilon_{lw}^{in}(\sigma) = \min \left(0.9.1 - \exp(-158W^{in}) \right),$$

with the incoming liquid water path

$$W^{in} = \int_{\sigma}^{z_T} \rho_a \min(0.0003, q_C) d\sigma.$$

Radiative heating and cooling at each model level are accounted for via the source term in the prognostic equation for temperature with

$$\left. \frac{\partial T}{\partial t} \right|_{RADIATION} = \left. \frac{\partial T}{\partial t} \right|_{RADIATION(clear-sky)} + \frac{1}{\rho c_p} \frac{\partial \Psi_{Heat}}{\partial \sigma} \frac{\partial \sigma}{\partial z},$$

where

$$\Psi_{Heat}(\sigma) = R_{sw(clear-sky)}^{in} \Psi_{Absorption} + R_{lw}^{in}(\sigma) - R_{lw}^{out}(\sigma),$$

with the incoming short-wave and long-wave components from the above expressions, and the outgoing long-wave radiation from

$$R_{lw}^{out}(\sigma) = R_{lw(clear-sky)}^{out} \left(1 - \varepsilon_{lw}^{out}(\sigma)\right) + \varepsilon_{lw}^{out}(\sigma)\sigma_{SB}T^{4}(\sigma),$$

$$\varepsilon_{lw}^{out}(\sigma) = \min\left(0.9, 1 - \exp\left(-130W^{out}\right)\right),$$

with the outgoing liquid water path $W^{out} = \int_{z_s}^{\sigma} \rho_a \min(0.0003, q_C) d\sigma$.

2.6 Surface boundary conditions

If the surface type is water, then the surface temperature is set equal to the water surface temperature, and surface moisture is set equal to the saturation value. If the surface type is permanent ice/snow, then the surface temperature is set equal to -10° C, and surface moisture is set equal to the saturation value.

If the surface type is land, then we assume that a single layer of vegetation overlays the soil (e.g. see Tuzet et al., 2003). Assuming a simple extinction approach to the attenuation of radiation through the vegetation, the contribution of radiation to the soil (subscript S) and vegetation (subscript V) is then

$$\begin{split} R_{sw,S} &= (1-\alpha_S)\tau R_{sw}^{in}, \\ R_{sw,V} &= (1-\alpha_V)(1-\tau)R_{sw}^{in}, \\ R_{lw,S} &= \tau R_{lw}^{in} + (1-\tau)\varepsilon_V \sigma_{SB}T_V^4 \cos\alpha_{Slope} - \varepsilon_S \sigma_{SB}T_S^4 \cos\alpha_{Slope}, \\ R_{lw,V} &= (1-\tau)R_{lw}^{in} + (1-\tau)\varepsilon_S \sigma_{SB}T_S^4 \cos\alpha_{Slope} - 2(1-\tau)\varepsilon_V \sigma_{SB}T_V^4 \cos\alpha_{Slope}, \\ \tau &= \exp(-0.4LAI), \end{split}$$

where α is surface albedo, ε is emissivity, LAI is the leaf area index and other variables and constants are defined in the previous Section. The extinction coefficient in the equation for τ takes on various values in the literature, but based on some initial sensitivity simulations with the model a value of 0.4 was chosen.

Total momentum, sensible heat and latent heat fluxes are then simply the sum of the soil and vegetation fluxes, the inverse of the total surface resistance is the sum of the component inverses, and surface temperature and specific humidity are weighted by the ratio of the total to component resistances.

2.6.1 Soil Scheme

Following Pielke (2002), the equations for soil temperature T_s , moisture content η_s and specific humidity q_s are

$$\begin{split} \frac{\partial T_{s}}{\partial t} &= \frac{\partial}{\partial \sigma} \left(K_{s} \frac{\partial T_{s}}{\partial \sigma} \right) \left(\frac{\partial \sigma}{\partial z} \right)^{2}, \\ \frac{\partial \eta_{s}}{\partial t} &= \frac{\partial}{\partial \sigma} \left(D_{\eta} \frac{\partial \eta_{s}}{\partial \sigma} \right) \left(\frac{\partial \sigma}{\partial z} \right)^{2} + \frac{\partial K_{\eta}}{\partial \sigma} \left(\frac{\partial \sigma}{\partial z} \right) + S_{\eta}, \end{split}$$

$$q_{S} = q_{S,sat} \exp\left(\frac{g\Psi_{\eta}}{R_{V}T_{S}}\right),$$

where subscript sat denotes the saturated value and

$$\begin{split} K_{s} &= k_{s} / (\rho_{s} c_{s}), \\ k_{s} &= \begin{cases} 419 \exp \left(-\left(\log_{10} \left(-100 \Psi_{\eta}\right) + 2.7\right)\right), & \text{if } \log_{10} \left(-100 \Psi_{\eta}\right) \leq 5.1, \\ 0.172, & \text{otherwise} \end{cases}, \\ \rho_{s} c_{s} &= (1 - \eta_{sat}) \rho_{s}^{dry} c_{s}^{dry} + \eta_{s} \rho_{w} c_{w}, \\ \rho_{w} &= 1000, \ c_{w} = 4186, \rho_{s}^{dry} = 1600, \ c_{s}^{dry} = 845, \end{split}$$

and where Ψ_{η} , K_{η} , D_{η} , η_{sat} , η_{wilt} are empirically derived constants or functions of soil moisture content and soil texture type as listed by Pielke (2002).

These equations are solved for 15 soil levels down to a depth of 2 m using an implicit vertical diffusion approach (see Section 4), with surface boundary condition for surface temperature

$$G_{S} = -k_{s} \frac{\partial T_{S}}{\partial \sigma} \frac{\partial \sigma}{\partial z},$$

and for soil moisture content

$$G_{\eta} = \rho_{w} D_{\eta} \frac{\partial \eta}{\partial \sigma} \frac{\partial \sigma}{\partial z} + \rho_{w} K_{\eta}$$

where

$$G_S = R_{S,sw} + R_{S,lw} - H_S - \lambda E_S + A_U,$$

$$G_{\eta} = -E_S + \rho_w (P - R)$$

$$H_S = \rho c_p (\theta_S - \theta_1) / r_{H,S} = \text{sensible heat flux (W m}^{-2}),$$

 $\lambda E_S = \rho \lambda (q_S - q_1) / r_{H,S} = \text{evaporative heat flux (W m}^{-2}),$
 $\lambda = 2.5 \times 10^6 \text{ J kg}^{-1},$

 $r_{\rm H,S}$ is the aerodynamic resistance (see Section 2.6.4) with a roughness length of 0.01 m,

P is precipitation reaching the soil and R is the runoff.

2.6.2 Vegetation parameterisation

The vegetation temperature T_{v} is calculated from a surface energy balance

$$0 = R_{sw,V} + R_{lw,V} - H_V - \lambda E_V$$

using Newton iteration, where the outward long-wave radiation and sensible (H_V) and latent (E_V) heat fluxes are treated as functions of T_V , with

$$H_{V} = \rho c_{p} (\theta_{V} - \theta_{1}) / r_{H,V},$$

$$E_{V} = (1 - \beta) E_{tr} + \beta E_{w},$$

$$E_{tr} = \rho (q_{V,sat} - q_{1}) / (r_{H,V} + r_{s}),$$

$$E_{w} = \rho (q_{V,sat} - q_{1}) / r_{H,V},$$

$$\beta = \begin{cases} 1; & \text{if condensation } (q_{1} > q_{V,sat}), \\ m_{r} / (0.0002LAI); & \text{if evapotranspiration} \end{cases},$$

$$\frac{\partial m_{r}}{\partial t} = P - P_{g} - \beta E_{w} / \rho_{w},$$

where m_r is the moisture reservoir and $r_{H,V}$ is the aerodynamic resistance (see Section 2.6.4).

The vegetation specific humidity q_V is calculated from $q_V = q_{V,sat} - E_V r_S / \rho$, and the stomatal resistance r_S is calculated using

$$r_S = \frac{r_{si}}{IAI} F_1 F_2^{-1} F_3^{-1} F_4^{-1}$$

and

$$F_1 = \frac{1+f}{f + (r_{si}/5000)}, \quad F_2 = \frac{\eta_d - \eta_{wilt}}{0.75\eta_{sat} - \eta_{wilt}},$$

$$F_3 = 1 - 0.00025(e_{V,sat} - e_1), \quad F_4 = 1 - 0.0016(298 - T_1)^2, \quad f = 0.55 \frac{R_{sw}^{in}}{R^*} \frac{2}{LAI}.$$

Other variables are

 $\alpha_V = \text{Vegetation albedo}(0.2),$

 $q_{V,sat}$ = Vegetation saturated specific humidity,

 $e_{V.sat}$ = Vegetation saturated vapour pressure,

$$R^* = \begin{cases} 30 \text{ W m}^{-2}; & \text{if } z_{0V} > 0.3\\ 100 \text{ W m}^{-2}; & \text{if } z_{0V} \le 0.3 \end{cases}$$

 z_{0V} = vegetation roughness length (m) = $h_V / 10$ (0.01 $\leq z_{0V} \leq 1.0$),

 h_V = vegetation height (m),

LAI = Leaf Area Index,

 $r_{si} = 50LAI = \text{minimum stomatal resistance (s}^{-1}).$

The vegetation (land-use) types used in TAPM are based on a CSIRO Wildlife and Ecology Categorisation (Graetz, 1998, personal communication), and are listed in Table 1, with urban/industrial conditions modified as described in Section 2.6.3.

Table 1: Vegetation (land-use) heights used in TAPM.

-1: Permanent snow/ice 0: Water 1: Forest – tall dense 2: Forest – tall mid-dense 3: Forest – dense 4: Forest – mid-dense 17.00 5: Forest – sparse (woodland) 6: Forest – very sparse (woodland) 7: Forest – low dense 8: Forest – low mid-dense 9: Forest – low sparse (woodland) 10: Shrub-land – tall mid-dense (scrub) 11: Shrub-land – tall sparse 12: Shrub-land – tall very sparse 13: Shrub-land – low mid-dense 15: Shrub-land – low sparse 16: Grassland – sparse hummock 17: Grassland – very sparse hummock 17: Grassland – very sparse hummock 18: Grassland – wery sparse tussock 20: Grassland – sparse tussock 20: Grassland – sparse tussock 21: Grassland – sparse tussock 22: Pasture/herb-field – dense (perennial) 23: Pasture/herb-field – mid-dense (perennial) 24: Pasture/herb-field – mid-dense (perennial) 25: Pasture/herb-field – mid-dense (perennial) 26: Pasture/herb-field – mid-dense (seasonal) 27: Pasture/herb-field – mid-dense (seasonal) 28: Littoral 29: Permanent lake 30: Ephemeral lake (salt) 31: Urban 32: Urban (low) 33: Urban (medium) 34: Urban (high) 35: Urban (cbd) 37: Industrial (medium) 37: Industrial (medium) 37: Industrial (medium)	Table 1: Vegetation (land-use) heights used in T	APM.
0: Water - 1: Forest – tall dense 42.00 2: Forest – tall mid-dense 36.50 3: Forest – dense 25.00 4: Forest – mid-dense 17.00 5: Forest – sparse (woodland) 12.00 6: Forest – very sparse (woodland) 10.00 7: Forest – low dense 9.00 8: Forest – low mid-dense 7.00 9: Forest – low sparse (woodland) 5.50 10: Shrub-land – tall mid-dense (scrub) 3.00 11: Shrub-land – tall mid-dense (scrub) 3.00 11: Shrub-land – tall very sparse 2.50 12: Shrub-land – low mid-dense 1.00 14: Shrub-land – low sparse 0.60 15: Shrub-land – low very sparse 0.50 16: Grassland – sparse hummock 0.50 17: Grassland – very sparse hummock 0.45 18: Grassland – wery sparse hummock 0.45 19: Grassland – sparse tussock 0.60 20: Grassland – sparse tussock 0.40 22: Pasture/herb-field – dense (perennial) 0.60 23: Pasture/herb-field – mid-dense (seasonal) 0.45	Vegetation Types:	$h_f(\mathbf{m})$
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	36: Industrial (low)	10.00
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38: Industrial (high) 10.00	38: Industrial (high)	10.00

2.6.3 Urban Parameterisation

The generic urban land-use category (31) contained in the default databases can be thought of as medium density urban conditions, with parameters specified in Table 2 based on Oke

(1988) and Pielke (2002). Other urban/industrial land-use categories listed in Table 2, not currently in the default databases, can also be selected through the model user interface (parameters for categories 32-35 are from McDonald Coutts, 2004, personal communication).

In urban regions the surface temperature and specific humidity are calculated using $T_0 = (1 - \sigma_U)T_{g\&f} + \sigma_UT_U$ and $q_0 = (1 - \sigma_U)q_{g\&f} + \sigma_Uq_U$, where σ_U is the fraction of urban cover, and subscript U denotes urban and g&f denotes the combined soil and foliage values respectively.

The equations for urban temperature T_U and specific humidity q_U use a similar approach as that for soil temperature, except that the surface properties are those of urban surfaces such as concrete/asphalt/roofs/etc:

$$\frac{\partial T_U}{\partial t} = \frac{3.72G_U}{\rho_U c_U d_U} - \frac{7.4(T_U - T_d)}{24 \times 3600},$$

$$q_U = 0,$$

where

$$G_U = R_{sw}^{in} (1 - \alpha_U) + R_{lw}^{in} - \varepsilon_U \sigma_{SB} T_U^4 \cos \alpha - H_U - \lambda E_U + A_U$$

= urban surface heat flux (W m⁻²),

$$H_U = \rho c_p (\theta_U - \theta_1) / r_H = \text{urban sensible heat flux (W m}^{-2}),$$

$$\lambda E_U = 0$$
 = urban evaporative heat flux (W m⁻²),

$$d_{\scriptscriptstyle U} = \sqrt{\frac{k_{\scriptscriptstyle U} \times 24 \times 3600}{\rho_{\scriptscriptstyle U} c_{\scriptscriptstyle U} \pi_{\scriptscriptstyle c}}} \,,$$

 A_U = urban anthropogenic heat flux (W m⁻²),

 $\varepsilon_U = 0.95 = \text{urban emissivity},$

$$\rho_U = 2300 \text{ kg m}^{-3} = \text{urban density},$$

$$c_U = 879 \,\mathrm{J \, kg^{-1} \, K^{-1}} = \text{urban heat capacity},$$

 α_U , k_U = urban albedo and conductivity.

Table 2: Urban/Industrial land-use characteristics used in TAPM.

Land-use Types:	$\sigma_{\scriptscriptstyle U}$	$lpha_{\scriptscriptstyle U}$	A_{U}	$k_{\scriptscriptstyle U}$	Z_{oU}
31: Urban	0.50	0.15	30	4.6	1.0
32: Urban (low)	0.50	0.17	20	1.5	0.4
33: Urban (medium)	0.65	0.15	30	5.0	0.6
34: Urban (high)	0.80	0.13	40	8.0	0.8
35: Urban (cbd)	0.95	0.10	70	10.0	2.0
36: Industrial (low)	0.50	0.15	50	4.6	0.5
37: Industrial (medium)	0.65	0.15	100	4.6	1.0
38: Industrial (high)	0.80	0.15	150	4.6	1.5

Note that the anthropogenic heat flux (A_U) is also included in the soil and vegetation surface flux equations when the land-use category is urban/industrial.

Urban surface layer scaling variables are calculated using the same approach as for soil and vegetation, incorporating the corresponding urban roughness length (z_{oU}) .

2.6.4 Surface fluxes and turbulence

Boundary conditions for the turbulent fluxes are determined by the modified Monin-Obukhov surface layer similarity of Luhar (2008, personal communication)

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$$\overline{w'u'}\Big|_{0} = -u_{*}^{2}u/\sqrt{u_{1}^{2} + v_{1}^{2}}, \quad \overline{w'v'}\Big|_{0} = -u_{*}^{2}v/\sqrt{u_{1}^{2} + v_{1}^{2}}, \quad \overline{w'\theta'_{v}}\Big|_{0} = -u_{*}\theta_{v*}, \quad \overline{w'q'}\Big|_{0} = -u_{*}q_{*}.$$

where

$$u_* = \begin{cases} k\sqrt{u_1^2 + v_1^2} / I_M, & \text{if } z/L < 0.4 \\ k\sqrt{u_1^2 + v_1^2} / J_M, & \text{if } z/L \ge 0.4 \end{cases},$$

$$\theta_{v^*} = k(\theta_{v1} - \theta_{v0})/I_H, \quad \theta_* = k(\theta_1 - \theta_0)/I_H, \quad q_* = k(q_1 - q_0)/I_H,$$

$$I_{M} = \begin{cases} \ln\left(\frac{z_{1}}{z_{0}}\right) - 2\ln\left(\frac{1 + \phi_{M}^{-1}(z_{1})}{1 + \phi_{M}^{-1}(z_{0})}\right) - \ln\left(\frac{1 + \phi_{M}^{-2}(z_{1})}{1 + \phi_{M}^{-2}(z_{0})}\right) \\ + 2\left(\tan^{-1}\left(\phi_{M}^{-1}(z_{1})\right) - \tan^{-1}\left(\phi_{M}^{-1}(z_{0})\right)\right), \text{ if } \frac{z_{1}}{L} < 0, \\ \ln\left(\frac{z_{1}}{z_{0}}\right) - \left(\phi_{M}(z_{1}) - \phi_{M}(z_{0})\right), & \text{ if } \frac{z_{1}}{L} \ge 0 \end{cases}$$

$$J_M = a \left(\frac{z}{L}\right)^b \left(1 - c\left(\frac{z}{L}\right)^{(1-b)}\right)$$
, with $a = 3.8$, $b = 0.5$ and $c = 0.3$,

$$I_H = I_{aH} + I_{bH},$$

$$I_{aH} = \begin{cases} \ln\left(\frac{z_1}{z_0}\right) - 2\ln\left(\frac{1 + \phi_H^{-1}(z_1)}{1 + \phi_H^{-1}(z_T)}\right), & \text{if } \frac{z_1}{L} < 0\\ \ln\left(\frac{z_1}{z_0}\right) - (\phi_H(z_1) - \phi_H(z_0)), & \text{if } \frac{z_1}{L} \ge 0 \end{cases},$$

$$I_{bH} = \ln \left(\frac{z_0}{z_T} \right),$$

$$r_{_{\! H}}=I_{_{\! H}}\,/(ku_*),\ r_{_{\! aH}}=I_{_{\! aH}}\,/(ku_*),\ r_{_{\! bH}}=I_{_{\! bH}}\,/(ku_*),$$

$$\phi_{M} = \begin{cases} \left(1 - 16\frac{z}{L}\right)^{-1/4}, & \text{for } \frac{z}{L} < 0\\ - \left(a_{1}\frac{z}{L} + b_{1}\left(\frac{z}{L} - \frac{c_{1}}{d_{1}}\right) \exp\left(-d_{1}\frac{z}{L}\right) + \frac{b_{1}c_{1}}{d_{1}}\right), & \text{for } \frac{z}{L} \ge 0 \end{cases}$$

$$\phi_{H} = \begin{cases} \left(1 - 16\frac{z}{L}\right)^{-1/2}, & \text{for } \frac{z}{L} < 0\\ - \left(\left(1 + \frac{2}{3}a_{1}\frac{z}{L}\right)^{1.5} + b_{1}\left(\frac{z}{L} - \frac{c_{1}}{d_{1}}\right) \exp\left(-d_{1}\frac{z}{L}\right) + \frac{b_{1}c_{1}}{d_{1}} - 1\right), & \text{for } \frac{z}{L} \ge 0 \end{cases}$$

$$\text{with } a_{1} = 1, b_{1} = 2/3, c_{1} = 5, d_{1} = 0.35,$$

$$\frac{z}{L} = \frac{kzg\theta_{v^{*}}}{u^{2}\theta}, & \text{and } z_{T} = z_{0}/7.4 & \text{from Garratt (1992)},$$

 $\frac{z}{L} = \frac{kzg\,\theta_{v^*}}{u_*^2\,\theta}$, and $z_T = z_0/7.4$ from Garratt (1992),

and the gradient Richardson number $R_{ig} = \frac{z}{L} \frac{\varphi_H}{\phi^2}$,

which in the stable limit gives a critical value of $R_{igc} = 0.2$

The above equations are also modified to include a zero-plane displacement height (z_d) by replacing z with z-z_d, where $z_d = \frac{20}{3}z_0$ for each surface (soil, vegetation, urban). These equations are solved iteratively, with the restrictions that $z_1 / L \le 1$ and $0.01 \le u_* \le 2.0$ m s⁻¹.

Turbulence boundary conditions are specified at the first model level using surface and mixed layer scaling, for the prognostic turbulence equations

$$E = c_m^{-1/2} u_*^2 + 0.5 w_*^2 \text{ and } \varepsilon = \frac{u_*^3}{kz} \phi_m - \frac{g}{\theta_u} u_* \theta_{v*},$$

where w_* is the convective velocity scale (m s⁻¹) defined as

$$w_* = \left(\frac{-gz_iu_*\theta_{v^*}}{\theta_v}\right)^{1/3},$$

and z_i is the convective boundary-layer height (m).

Initial conditions and boundary conditions 2.7

The model is initialised at each grid point with values of $u_s, v_s, \theta_{vs}, q_s$ interpolated from the synoptic analyses. Iso-lines of these variables are oriented to be parallel to mean sea level (i.e. cutting into the terrain). Turbulence levels are set to their minimum values as the model is started at midnight. The Exner pressure function is integrated from mean sea level to the model top to determine the top boundary condition. The Exner pressure and terrain-following vertical velocity are then diagnosed using equations (3) and (5) respectively. Surface temperature and moisture are set to the deep soil values specified, with surface temperature adjusted for terrain height using the synoptic lapse rate. At the model top boundary, all variables are set at their synoptic values.

One-way nested lateral boundary conditions are used for the prognostic equations (1), (2), (4), and (7) using an approach based on Davies (1976). For example for u, an additional term is added to the right hand side of equation (1).

$$\frac{du}{dt} = RHS(u) - F_{NEST} \frac{(u - \widetilde{u})}{3\Delta t}$$

where \tilde{u} is interpolated from the coarse outer grid onto the fine inner grid, and

$$F_{NEST} = \max(G_x, G_y)$$

$$\begin{cases} 1 - \left(\frac{i-1}{n_b}\right)^2; & \text{for } i = 1, ..., n_b; \\ 1 - \left(\frac{n_x - i}{n_b}\right)^2; & \text{for } i = n_x - (n_b - 1), ..., n_x; \\ 0; & \text{otherwise.} \end{cases}$$

and similarly for G_y , with n_x the number of grid points in the x direction, and $n_b = 5$ the number of grid points in from the grid edge over which the solutions are meshed. On the outer grid, this same nesting procedure is used, but using time-interpolated synoptic winds, temperature and moisture. Note that the terrain is smoothed near the lateral boundaries to reduce noise created by the boundary conditions.

2.8 Assimilation of wind observations

The method used to optionally assimilate wind observations is based on the approach of Stauffer and Seaman (1994), where a nudging term is added to the horizontal momentum equations (for u and v). The equation for u is

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$$\frac{\partial u}{\partial t} = RHS(u) + G\left(\frac{\sum_{n=1}^{nsite} W_n (u_n - \hat{u}_n)}{\sum_{n=1}^{nsite} W_n}\right),$$

where

 $G = \text{nudging coefficient} = 1/(3\Delta t),$

 Δt = model meteorological advection timestep,

 u_n = observed u at observation site n,

 $\hat{u}_n = \text{model } u \text{ interpolated to observation site } n$,

$$W_n = \begin{cases} Q_n \left(\frac{R_n^2 - D_n^2}{R_n^2 + D_n^2} \right); & \text{if } D_n < R_n; \\ 0; & \text{otherwise.} \end{cases}$$

 $Q_n = \text{data quality indicator } [0...1],$

 R_n = radius of influence (m),

$$D_n^2 = (x_i - x_n)^2 + (y_j - y_n)^2,$$

 (x_i, y_j) = location of grid point,

 (x_n, y_n) = location of observation site.

Note that observations at any height can be included, and the observations can influence a user-specified number of model levels for each site.

3 Air pollution component

3.1 Eulerian grid module

The Eulerian Grid Module (EGM) consists of nested grid-based solutions of the Eulerian concentration mean and optionally variance equations representing advection, diffusion, chemical reactions and emissions. Dry and wet deposition processes are also included.

3.1.1 Pollutant equations

The prognostic equation for concentration χ is similar to that for the potential virtual temperature and specific humidity variables, and includes advection, diffusion, and terms to represent pollutant emissions S_{γ} and chemical reactions R_{γ}

$$\frac{d\chi}{dt} = \frac{\partial}{\partial x} \left(K_{H\chi} \frac{\partial \chi}{\partial x} \right) + \frac{\partial}{\partial y} \left(K_{H\chi} \frac{\partial \chi}{\partial y} \right) - \left(\frac{\partial \sigma}{\partial z} \right) \frac{\partial}{\partial \sigma} \left(\overline{w'\chi'} \right) + S_{\chi} + R_{\chi}$$
(16)

where

$$\overline{w'\chi'} = -K_{\chi} \frac{\partial \chi}{\partial \sigma} \frac{\partial \sigma}{\partial z}$$

and with diffusion coefficients $K_{H\chi} = \min(10, K_{\chi})$ and $K_{\chi} = 2.5K$.

In tracer mode, or for SO₂ in chemistry mode, concentration variance $\overline{\chi'^2}$ can be computed using the following prognostic equation:

$$\frac{d\overline{\chi'^{2}}}{dt} = \frac{\partial}{\partial x} \left(K_{H\chi} \frac{\partial \overline{\chi'^{2}}}{\partial x} \right) + \frac{\partial}{\partial y} \left(K_{H\chi} \frac{\partial \overline{\chi'^{2}}}{\partial y} \right) + \left(\frac{\partial \sigma}{\partial z} \right)^{2} \frac{\partial}{\partial \sigma} \left(K_{\chi} \frac{\partial \overline{\chi'^{2}}}{\partial \sigma} \right) + P_{V} - \varepsilon_{V} + S_{V} \tag{17}$$

with production term

$$P_{V} = \begin{cases} 2K_{\chi} \Biggl(\Biggl(\frac{\partial \overline{\chi}}{\partial x} + \frac{\partial \overline{\chi}}{\partial \sigma} \frac{\partial \sigma}{\partial x} \Biggr)^{2} + \Biggl(\frac{\partial \overline{\chi}}{\partial y} + \frac{\partial \overline{\chi}}{\partial \sigma} \frac{\partial \sigma}{\partial y} \Biggr)^{2} + \Biggl(\frac{\partial \overline{\chi}}{\partial \sigma} \frac{\partial \sigma}{\partial z} \Biggr)^{2} \Biggr), & \text{if } \overline{\chi} \text{ in EGM mode;} \\ 2c_{k(LPM)} K \Biggl(\Biggl(\frac{\partial \overline{\chi}}{\partial x} + \frac{\partial \overline{\chi}}{\partial \sigma} \frac{\partial \sigma}{\partial x} \Biggr)^{2} + \Biggl(\frac{\partial \overline{\chi}}{\partial y} + \frac{\partial \overline{\chi}}{\partial \sigma} \frac{\partial \sigma}{\partial y} \Biggr)^{2} + \Biggl(\frac{\partial \overline{\chi}}{\partial \sigma} \frac{\partial \sigma}{\partial z} \Biggr)^{2} \Biggr), & \text{if } \overline{\chi} \text{ in LPM mode;} \end{cases}$$

concentration variance dissipation rate

$$\varepsilon_{\chi} = \frac{2}{c_{\chi}} \frac{\varepsilon}{E} \overline{\chi'^{2}},$$

the emission source term

$$S_V = 2I_E \left(\overline{\chi'^2} \right)^{1/2} S_{\chi},$$

and with the emission concentration fluctuation intensity set to $I_E = 0.5$ for all sources.

The constant $c_{\chi} = 1.6$ is based on that used by Rodi (1985), while $c_{k(LPM)} = 0.3$ represents the scalar diffusivity coefficient when LPM mean concentration is used. Ideally, concentration

variance should be calculated using a Lagrangian approach when in LPM mode, but nevertheless, results from the current approach give good near-source concentration variance for point sources in LPM mode. The concentration variance χ'^2 is initially set to zero and uses zero gradient boundary conditions on all grids.

The calculation of peak-to-mean concentration is performed when pollution is post-processed. The maximum hourly-averaged concentration is enhanced to obtain peak concentration estimates for 10-minute, 3-minute, 1-minute and 1-second averaging periods. Peak concentrations are calculated using the commonly used power-law relationship, but with an exponent that depends on concentration fluctuation intensity $I_{\rm C}$ (derived from the mean and variance of the concentration output from the model)

$$C_{MAX}(t) = C_{MAX}(3600) \left(\frac{3600}{t}\right)^{\min(0.1+0.25I_C^{1/3},0.4)},$$

with t the averaging period (s), and

$$I_C = \left(\frac{\overline{\chi'^2}}{\overline{\chi}^2}\right)^{1/2}.$$

Note that the peak-to-mean approach is only valid for long time-series, and is typically used for results from annual model runs.

3.1.2 Chemistry and Aerosols

The model can be run in either tracer mode, chemistry mode, or dust mode. In tracer mode, the only chemical reaction is an optional exponential decay $R_{\chi} = -k_{decay}\chi$, where the decay rate k_{decay} is a model input. In chemistry mode, gas-phase photochemistry is based on the semi-empirical mechanism called the Generic Reaction Set (GRS) of Azzi et al. (1992), with the hydrogen peroxide modification of Venkatram et al. (1997). We have also included gas-and aqueous-phase reactions of sulfur dioxide and particles, with the aqueous-phase reactions based on Seinfeld and Pandis (1998). In dust mode, pollutant concentration is calculated for four particle size ranges: $PM_{2.5}$, PM_{10} , PM_{20} and PM_{30} . The emissions, background concentrations and output concentrations are relevant for these four categories, while calculations in the model are actually done for $PM_{2.5}$, PM_{10} , PM_{10-20} and PM_{20-30} . This categorisation allows representative particle sizes to be used to account for particle settling and dry/wet deposition. Exponential decay of particles is also allowed, as is available in tracer mode, but there are no chemical transformations or particle growth processes included.

In chemistry mode, there are ten reactions for thirteen species: smog reactivity (R_{smog}), the radical pool (RP), hydrogen peroxide (H_2O_2), nitric oxide (NO), nitrogen dioxide (NO₂), ozone (O₃), sulfur dioxide (SO₂), stable non-gaseous organic carbon (SNGOC), stable gaseous nitrogen products (SGN), stable non-gaseous nitrogen products (SNGN), stable non-gaseous sulfur products (SNGS), plus Airborne Particulate Matter (APM) and Fine Particulate Matter (FPM) that include secondary particulate concentrations consisting of (SNGOC), (SNGN), and (SNGS).

The reactions are

The reactions are	
Reactions	Reaction Rates
$R_{smog} + h\nu \rightarrow RP + R_{smog} + \eta SNGOC$	$R_1 = k_1 [R_{smog}]$
$RP + NO \rightarrow NO_2$	$R_2 = k_2[RP][NO]$
$NO_2 + hv \rightarrow NO + O_3$	$R_3 = k_3[NO_2]$
$NO + O_3 \rightarrow NO_2$	$R_4 = k_4[NO][O_3]$
$RP + RP \rightarrow RP + \alpha H_2 O_2$	$R_5 = k_5[RP][RP]$
$RP + NO_2 \rightarrow SGN$	$R_6 = k_6[RP][NO_2]$
$RP + NO_2 \rightarrow SNGN$	$R_7 = k_7 [RP][NO_2]$
$RP + SO_2 \rightarrow SNGS$	$R_8 = k_8[RP][SO_2]$
$H_2O_2 + SO_2 \rightarrow SNGS$	$R_9 = k_9 [H_2 O_2][SO_2]$
$O_3 + SO_2 \rightarrow SNGS$	$R_{10} = k_{10}[O_3][SO_2]$

where [A] denotes concentration of species A and hv denotes photo-synthetically active radiation.

Yield coefficients are

$$\alpha = \max \left(0.03, \exp \left(-0.0261 \frac{[R_{smog}]}{[NO_X]} \right) \right),$$

$$\eta = 0.1,$$

and reaction rate coefficients are

$$\begin{split} k_1 &= k_3 f, \\ k_2 &= 3580/(60T), \\ k_3 &= 0.0001 \delta .TSR/60, \\ k_4 &= (924/60T) \exp(-1450/T), \\ k_5 &= (10/60), \\ k_6 &= (0.12/60), \\ k_7 &= k_6, \\ k_8 &= (0.003/60), \\ k_9 &= \frac{7.45 \times 10^7 [H^+] \alpha_1}{1 + 13 [H^+]} K_{H_-S(IV)} K_{H_-H_2O_2} L \cdot R \cdot T \cdot 10^{-9}, \\ k_{10} &= (2.4 \times 10^4 \alpha_0 + 3.7 \times 10^5 \alpha_1 + 1.5 \times 10^9 \alpha_2) K_{H_-S(IV)} K_{H_-O_3} L \cdot R \cdot T \cdot 10^{-9}, \end{split}$$

with

$$[H^{+}] = 10^{-pH},$$

$$\alpha_{0} = \frac{K_{H0_SO_{2}}}{K_{H_S(IV)}}, \alpha_{1} = \alpha_{0} \frac{K_{H1_SO_{2}}}{[H^{+}]}, \alpha_{2} = \alpha_{1} \frac{K_{H2_SO_{2}}}{[H^{+}]},$$

$$K_{H_S(IV)} = K_{H0_SO_{2}} \left(1 + \frac{K_{H1_SO_{2}}}{[H^{+}]} \left(1 + \frac{K_{H2_SO_{2}}}{[H^{+}]}\right)\right),$$

$$K_{H0_SO_{2}} = 1.24 \exp\left(-3120 \left(\frac{1}{298} - \frac{1}{T}\right)\right),$$

$$K_{H1_SO_{2}} = 1.29 \times 10^{-2} \exp\left(-2080 \left(\frac{1}{298} - \frac{1}{T}\right)\right),$$

$$K_{H2_SO_{2}} = 6.014 \times 10^{-8} \exp\left(-1120 \left(\frac{1}{298} - \frac{1}{T}\right)\right),$$

$$K_{H_{2}_SO_{2}} = 7.1 \times 10^{4} \exp\left(-7250 \left(\frac{1}{298} - \frac{1}{T}\right)\right),$$

$$K_{H_{2}O_{3}} = 9.4 \times 10^{-3} \exp\left(-2520 \left(\frac{1}{298} - \frac{1}{T}\right)\right),$$

$$(all \ K_{H} \le (L \cdot R \cdot T)^{-1}),$$

where APM and FPM are in μ g m⁻³, all other species are in units of ppb, the rate coefficients k_1, k_3 are in s⁻¹ and $k_2, k_4, k_5, k_6, k_7, k_8, k_9, k_{10}$ are in ppb⁻¹ s⁻¹, temperature T is in K, the total solar radiation TSR is in W m⁻², R is the gas constant (0.082) in atm M⁻¹ K⁻¹, L is the volume based liquid water fraction related to the liquid water specific humidity by $L = q_L \rho / \rho_W$,

$$f = \exp\left(-4700\left(\frac{1}{T} - \frac{1}{316}\right)\right),$$

$$\delta = \begin{cases} 4.23 + 1.09 / \cos Z; & \text{if } 0 \le Z \le 47\\ 5.82; & \text{if } 47 \le Z \le 64, \\ -0.997 + 12(1 - \cos Z); & \text{if } 64 \le Z \le 90 \end{cases}$$

and Z is the zenith angle in degrees.

The yield factor η , the reaction rate k_8 , and the secondary formation of APM and FPM by the various processes, are in a preliminary form that needs to be verified against appropriate data.

The concept of using R_{smog} rather than Volatile Organic Compounds (VOCs) in the reaction equations follows from the work of Johnson (1984). The concentration of R_{smog} is defined as a reactivity coefficient multiplied by VOC concentration. For example, Johnson (1984) used $[R_{smog}] = 0.0067[VOC]$ for typical 1980s Australian urban air dominated by motor vehicles. Empirically determined reactivity coefficients for individual VOC species are available from smog chamber experiments, while numerically determined reactivity coefficients have been calculated by comparison of the GRS mechanism with more complex mechanisms (Cope, 1999, personal communication).

Table 3: Characteristics of the CBIV lumped VOC species needed for the GRS mechanism

(Cope, 1999, personal communication).

CBIV Lumped VOC	Carbon	Molecular	CBIV
Species (i)	Number	Weight	Reactivity
	(CN_i)	(MW_i)	(a_i) (ppb
			ppbC ⁻¹)
			(URBAN)
Formaldehyde (FORM) (CH ₂ 0)	1	30	0.0174
Higher Aldehydes (ALD2) (C ₂ H ₄ 0)	2	44	-0.00081
Ethene (ETH) (C_2H_4)	2	28	0.0153
Alkenes (Olefins) (OLE) (C ₂ H ₄)	2	28	0.0127
Alkanes (Paraffins) (PAR) (CH ₂)	1	14	0.00095
Toluene (TOL) (C ₇ H ₈)	7	92	0.0049
Xylene (XYL) (C_8H_{10})	8	106	0.0145
Isoprene (ISOP) (C ₅ H ₈)	5	68	0.0092

Emissions from VOC sources usually consist of more than one type of VOC, necessitating the R_{smog} emission rate to be calculated in the following way

$$Q_{Rsmog} = \sum_{i} \frac{14CN_{i}}{MW_{i}} a_{i} Q_{i} ,$$

where Q_i is the emission rate (g s⁻¹) for each VOC, a_i is its reactivity, CN_i is its carbon number and MW_i is its molecular weight. An alternative (and more precise) approach is to use a standard reactivity coefficient for a standard VOC mixture (for example $Q_{Rsmog} = 0.0067Q_{VOC}$) with perturbations about this standard accounted for using the individual species reactivity coefficients (M. Cope, 1999, personal communication). Sample perturbation coefficients for the Carbon Bond IV (CBIV) and the updated Carbon Bond IV (CBIV_99) mechanisms are summarised in Tables 3 and 4 respectively. More detail on the perturbation coefficients summarised in Table 4 are given in Hurley et al., (2003).

Table 4: Characteristics of the CBIV_99 lumped VOC species needed for the GRS machanism (Copp. 2003, personal communication)

mechanism (Cope, 2003, personal communication).

CBIV Lumped VOC	Carbon	Molecular	CBIV_99	CBIV_99
Species (i)	Number	Weight	Reactivity	Reactivity
	(CN_i)	(MW_i)	(a_i) (ppb	(a_i) (ppb
			ppbC ⁻¹)	ppbC ⁻¹)
			(URBAN)	(RURAL)
Formaldehyde (FORM) (CH ₂ 0)	1	30	0.0350	0.0350
Higher Aldehydes (ALD2) (C ₂ H ₄ 0)	2	44	0.0100	0.0150
Ethene (ETH) (C_2H_4)	2	28	0.0070	0.0140
Alkenes (Olefins) (OLE) (C ₂ H ₄)	2	28	0.0080	0.0180
Alkanes (Paraffins) (PAR) (CH ₂)	1	14	0.0000	0.0005
Toluene (TOL) (C ₇ H ₈)	7	92	0.0008	0.0016
Xylene (XYL) (C_8H_{10})	8	106	0.0080	0.0140
Isoprene (ISOP) (C ₅ H ₈)	5	68	0.0090	0.0300

If we define $[NO_X] = [NO] + [NO_2]$ and $[SP_X] = [O_3] + [NO_2]$ (analogous to the definition of smog produced by Johnson, 1984, but without including SGN and SNGN), we do not need the differential equations for NO and O₃. The resulting reaction terms for the prognostic equation (11) for the nine pollutants APM, FPM, SO₂, NO_X, R_{smog}, SP_X, NO₂, RP, and H₂O₂ are

$$\begin{split} R_{\text{[APM]}} &= F_{\text{CH2}} \eta R_1 + F_{\text{HNO3}} R_7 + F_{\text{H2SO4}} \left(R_8 + R_9 + R_{10} \right) \\ R_{\text{[FPM]}} &= F_{\text{CH2}} \eta R_1 + 0.5 F_{\text{HNO3}} R_7 + F_{\text{H2SO4}} \left(R_8 + R_9 + R_{10} \right) \\ R_{\text{[SO_2]}} &= -R_8 - R_9 - R_{10} \\ R_{\text{[NO_X]}} &= -R_6 - R_7 \\ R_{\text{[R_{smog}]}} &= 0 \\ R_{\text{[SP_X]}} &= R_2 - R_6 - R_7 - R_{10} \\ R_{\text{[NO_2]}} &= R_2 - R_3 + R_4 - R_6 - R_7 \\ R_{\text{[RP]}} &= R_1 - R_2 - R_5 - R_6 - R_7 - R_8 \\ R_{\text{[H_{2O_2]}}} &= \alpha R_5 - R_9 \end{split}$$

where $F_{HNO3} = 2.6$, $F_{H2SO4} = 4.0$, $F_{CH2} = 0.57$, are approximate factors to convert the stable non-gaseous compounds to APM in $\mu g \ m^{-3}$ at NTP.

The potentially fast reactions in the reduced system are for SO_2 , NO_2 , RP, and H_2O_2 . This implies that a small explicit timestep is necessary, but this restriction can be overcome by using a simple implicit solution procedure described later. This approach then allows large numerical time-steps to be used, provided the pH of the liquid water present is below about 5.5 (so that the reaction between O_3 and SO_2 to produce SNGS (R_{IO}) does not dominate the aqueous phase reactions). Note that the default pH of the liquid water present in the model is 4.5, which is typical of Australian conditions.

3.1.3 Deposition and Particle Settling

The dry deposition formulation for gaseous pollutants follows that of Physick (1994) in which all scalars behave like heat in terms of roughness length and stability function. Knowing the resistance functions for heat transfer r_{aH} and r_{bH} (Section 2.6.4), and the stomatal resistance r_s (Section 2.6.2), the surface flux for variable χ is written as $\overline{w'\chi'}|_{o} = -\chi_1 V_d$, where the pollutant deposition velocity is $V_d = (r_{aero} + r_{surface})^{-1}$, the aerodynamic resistance is $r_{aero} = r_{aH} + r_{bH} Sc^{2/3}$, the surface resistance $r_{surface}$ depends on the surface type, and Sc is the Schmidt Number (the ratio of the molecular diffusivities for water vapour and pollutant concentration).

For a land surface,
$$V_d = \frac{\sigma_f \beta}{r_{aero} + r_{water}} + \frac{\sigma_f (1 - \beta)}{r_{aero} + r_S Sc} + \frac{(1 - \sigma_f)}{r_{aero} + r_{soil}}$$

and for a water surface, $V_d = \frac{1}{r_{aero} + r_{water}}$.

Non-zero deposition velocities are used for the gaseous pollutants NO_2 , NO, O_3 , SO_2 and H_2O_2 , with resistance values based on information in Wesley (1989) and Harley et al. (1993)

NO₂:
$$r_{water} = 1500, r_{soil} = 500, Sc = \sqrt{46/18}$$
,
NO: $r_{water} = 10000, r_{soil} = 10000, Sc = \sqrt{30/18}$;
O₃: $r_{water} = 2000, r_{soil} = 400, Sc = \sqrt{48/18}$;
SO₂: $r_{water} = 0, r_{soil} = 1000, Sc = \sqrt{64/18}$;
H₂O₂: $r_{water} = 0, r_{soil} = 100, Sc = \sqrt{34/18}$.

The method for calculating the dry deposition velocity for aerosols is based on the approach of Seinfeld and Pandis (1998). The deposition velocity is calculated using $V_d = \frac{1}{r_{aH} + r_{bH} + r_{aH} r_{bH} V_S} + V_S$, where the resistance functions for heat transfer r_{aH} and r_{bH} and the particle settling velocity V_S are known, and the surface (water, soil, stomatal) resistance is assumed to be zero.

The quasi-laminar resistance r_{bH} accounts for Schmidt number (Sc) and Stokes number (St) dependence as follows:

$$r_{bH} = \frac{1}{u_* \left(Sc^{-2/3} + 10^{-3/St} \right)}$$

with

$$Sc = v/D$$
,
 $v = 1.58 \times 10^{-5} \text{ m}^2 \text{ s}^{-1}$,

$$D = \text{diffusivity of species} = \begin{cases} 1.00 \times 10^{-12} \text{ m}^2 \text{ s}^{-1} \text{ for PM}_{20\text{-}30}, \\ 1.90 \times 10^{-12} \text{ m}^2 \text{ s}^{-1} \text{ for PM}_{10\text{-}20}, \\ 6.10 \times 10^{-12} \text{ m}^2 \text{ s}^{-1} \text{ for PM}_{10} \text{ or APM}, \\ 2.74 \times 10^{-11} \text{ m}^2 \text{ s}^{-1} \text{ for PM}_{2.5} \text{ or FPM}, \end{cases}$$

and

$$St = \frac{V_S u_*^2}{g V},$$

$$V_S = \frac{g C_C \rho_P D_P^2}{18 \mu},$$

with

$$g = 9.81 \,\mathrm{m \, s^{-2}}, \; \rho_P = 1000 \,\mathrm{kg \, m^{-3}}, \; \mu = 1.8 \times 10^{-5} \,\mathrm{kg \, m^{-1} \, s^{-1}},$$

$$C_C = \begin{cases} 1.01 \text{ for PM}_{20\text{-}30}, \\ 1.01 \text{ for PM}_{10\text{-}20}, \\ 1.05 \text{ for PM}_{10} \text{ or APM}, \\ 1.16 \text{ for PM}_{2.5} \text{ or FPM}. \end{cases}$$

$$D_{P} = \text{representative particle aerodynamic diameter} = \begin{cases} 25 \, \mu \text{m for PM}_{20\text{-}30}, \\ 15 \, \mu \text{m for PM}_{10\text{-}20}, \\ 4 \, \mu \text{m for PM}_{10} \text{ or APM}, \\ 1 \, \mu \text{m for PM}_{25} \text{ or FPM}. \end{cases}$$

For aerosol concentrations such as FPM and APM in chemistry mode or for PM_{2.5}, PM₁₀, PM₁₀₋₂₀ and PM₂₀₋₃₀ in dust mode, particle settling in EGM mode is performed using an extra vertical advection term in the prognostic equations for each species, with downward velocity V_s (scaled to be in the terrain-following coordinate system).

Wet deposition in chemistry or dust mode is important only for highly soluble gases and aerosols. For the pollutants considered in this model, the only ones removed by wet processes are SO_2 , and H_2O_2 , FPM (PM_{2.5}), APM (PM₁₀), PM₂₀, and PM₃₀.

For the gases SO₂ and H₂O₂, the amount of each pollutant dissolved in the rain-water fraction of the liquid water is computed for pollutant A as $[A]_R = (L_R R T K_{H_A})[A]$, where $L_R = q_R \rho / \rho_W$ is the liquid rain-water volume fraction, R is the gas constant (0.082) in atm M⁻¹ K⁻¹, T is temperature in K, K_{H_A} is the effective Henry's Law coefficient for A, and concentrations are in ppb. $[A]_R$ is then vertically advected at the speed of the falling rain (V_T) , to give $[A]_{R(NEW)}$. The new value of A is then $[A]_{(NEW)} = [A] - [A]_R + [A]_{R(NEW)}$.

For aerosols, the same approach is used as for the gases, except that we assume $K_{H_{-}A} = K_{H_{-}MAX} = (L_{T}RT)^{-1}$ (i.e. that all particles are dissolved in the available water), with the total liquid water volume fraction $L_{T} = (q_{C} + q_{R})\rho/\rho_{W}$.

In tracer mode, a number of species with non-zero deposition characteristics can be selected individually for each tracer, with dry deposition characteristics:

SO₂:
$$r_{water} = 0, r_{soil} = 1000, Sc = \sqrt{64/18};$$

HF: $r_{water} = 0, r_{soil} = 100, Sc = \sqrt{20/18}.$

Both of these species are assumed to be readily dissolved in water, and so totally removed by wet deposition. This assumption for sulfur dioxide is different to that used in chemistry mode, as other species needed to calculate the amount dissolved in the available liquid water (e.g. hydrogen peroxide and ozone) are not available in tracer mode.

3.1.4 Emission correction factors

A range of pollutant emissions types can be used by the model. They include point sources, line sources, area sources and gridded surface sources. TAPM expects the seven optional gridded surface emission files to be in the following forms

- Gridded Surface Emissions (GSE), independent of meteorology;
- Biogenic Surface Emissions (BSE), at $T_{vege} = 30^{\circ}\text{C}$, $PAR = 1000 \,\mu\text{mol m}^{-2} \,\text{s}^{-1}$ for VOC, and at $T_{soil} = 30^{\circ}\text{C}$ for NO_X;
- Wood Heater Emissions (WHE), at $T_{screen24} = 10^{\circ}$ C for all pollutant species;
- Vehicle Petrol eXhaust emissions (VPX), at $T_{screen} = 25^{\circ}$ C for VOC, NO_X and CO;
- Vehicle Diesel eXhaust emissions (VDX), independent of meteorology;
- Vehicle Lpg eXhaust emissions (VLX), at $T_{screen} = 25$ °C for VOC, NO_X and CO;
- Vehicle Petrol eVaporative emissions (VPV), at $T_{screen} = 25$ °C for VOC;

where T_{vege} is the vegetation temperature (°C), T_{soil} is the soil temperature (°C), PAR is the photo-synthetically active radiation (µmol m⁻² s⁻¹), $T_{screen24}$ is a running 24-hour screen-level temperature (°C), and T_{screen} is the screen-level temperature (°C). The model adjusts the emissions throughout a simulation, according to predicted temperature and PAR.

The biogenic temperature and radiation corrections are from Guenther et al. (1993) for VOC and from Williams et al. (1992) for NO_X. The wood heater and vehicle temperature corrections used in the model are based on curve-fits to data described by Ng et al. (2000), which for vehicle emissions are based on the US model MOBILE5.

The temperature and radiation corrections for BSE VOC emissions are

$$C_{T} = \frac{\exp\left(\frac{95000(T - 303.15)}{303.15RT}\right)}{1 + \exp\left(\frac{230000(T - 314)}{303.15RT}\right)},$$

$$C_{PAR} = \frac{1.066(0.0027PAR)}{\sqrt{1 + (0.0027PAR)^{2}}},$$

with

$$T = T_{vege} + 273.15,$$

$$R = 8.314 \,\mathrm{J \, K^{-1} \, mol^{-1}}$$

$$PAR = 4.18 \cdot (0.55 \cdot TSR)$$
 in μ mol m⁻² s⁻¹,

$$TSR = \text{total solar radiation (W m}^{-2}).$$

The temperature correction for BSE NO_X emissions is

$$NO_X$$
, NO_2 : $C_T = \exp(0.071(T - 303.15))$,

with
$$T = T_{soil} + 273.15$$
.

The temperature correction for WHE emissions for all pollutant species is

$$C_T = \max(0, 2 - 0.1T_{screen24}).$$

The temperature corrections for VPX and VLX emissions are

$$\text{VOC:} \quad C_T = \begin{cases} 1 - 0.03(T_{screen} - 25), \text{ if } T_{screen} < 25^{\circ}\text{C} \\ 1 + 0.02(T_{screen} - 25), \text{ if } T_{screen} \geq 25^{\circ}\text{C} \end{cases};$$

NOX:
$$C_T = \begin{cases} 1 - 0.0125(T_{screen} - 25), & \text{if } T_{screen} < 25^{\circ}\text{C} \\ 1 - 0.0025(T_{screen} - 25), & \text{if } T_{screen} \ge 25^{\circ}\text{C} \end{cases}$$

$$\text{CO:} \quad C_T = \begin{cases} 1 - 0.02 (T_{screen} - 25), \text{ if } T_{screen} < 25^{\circ}\text{C} \\ 1 + 0.04 (T_{screen} - 25), \text{ if } T_{screen} \ge 25^{\circ}\text{C} \end{cases}.$$

The temperature correction for VPV emissions is

VOC:
$$C_T = \begin{cases} \max(0.01,1+0.05(\min(T_{screen},41)-27)), & \text{if } T_{screen} < 27^{\circ}\text{C} \\ \max(0.01,1+0.20(\min(T_{screen},41)-27)), & \text{if } T_{screen} \ge 27^{\circ}\text{C} \end{cases}$$

3.2 Lagrangian particle module

The Lagrangian Particle Module (LPM) can be used on the inner-most nest for selected point sources to allow a more detailed account of near-source effects, including gradual plume rise and near-source dispersion. The LPM uses a PARTPUFF approach as described by Hurley (1994), whereby mass is represented as a puff in the horizontal direction, and as a particle in the vertical direction. This configuration has been used successfully in the Lagrangian Atmospheric Dispersion Model (LADM, Physick et al., 1994). Chemistry is accounted for in a straightforward coupled manner with the EGM, without having to convert secondary pollutant concentration back to particle mass. This is done by tracking primary emissions for a particular source with the LPM and accounting for reactions using the EGM (see later). Deposition processes are neglected in the LPM. Once particles have travelled for a certain length of time (model input), the particle is no longer tracked and its mass is converted to concentration and put onto the EGM grid.

3.2.1 Pollutant equations

In the horizontal directions, particle position is updated through advection by the ambient wind, with diffusion accounted for through a puff width relation based on statistical diffusion theory

$$\frac{d\sigma_y^2}{dt} = 2\left(\sigma_u^2 + \sigma_{up}^2\right)T_{Lu}\left(1 - \exp\left(-\frac{t}{T_{Lu}}\right)\right),$$

where

 $\sigma_u^2, \sigma_{up}^2$ are the ambient and plume rise horizontal velocity variances respectively,

$$\sigma_u^2 = \min(0.04, E - \frac{1}{2}\overline{w'^2})$$

 σ_{up}^2 is specified in Section 3.3,

$$T_{Lu} = \frac{2\sigma_u^2}{C_0 \varepsilon}$$
 is the ambient horizontal Lagrangian timescale,

and $C_0 = 3.0$.

In the vertical direction, particle position is updated using

$$\frac{d\sigma_{particle}}{dt} = \dot{\sigma} + \dot{\sigma}' + \dot{\sigma}'_{p},$$

where

 $\sigma_{\it particle}$ is the particle position in terrain following coordinates,

 $\dot{\sigma}$ is the mean ambient vertical velocity,

 $\dot{\sigma}'$ is the perturbation of vertical velocity due to ambient turbulence,

 $\dot{\sigma}'_{p}$ is the perturbation of vertical velocity due to plume rise effects.

Perfect reflection of particle vertical position and velocity is used at the ground.

The perturbation of vertical velocity due to ambient turbulence is determined from the solution of a Langevin equation using a non-stationary turbulence extension of the approach of Franzese et al. (1999)

$$\dot{\sigma}' = w' \frac{\partial \sigma}{\partial z},$$

$$dw' = (a_0 + a_1 w' + a_2 w'^2) dt + b_0 \xi,$$

where ξ is a random number from a Gaussian distribution with mean zero and variance one, and

$$b_{0} = \sqrt{C_{0}\varepsilon dt},$$

$$a_{2} = \frac{\frac{1}{3}\left(\frac{\partial \overline{w'^{3}}}{\partial t} + \frac{\partial \overline{w'^{4}}}{\partial z}\right) - \frac{\overline{w'^{3}}}{2\overline{w'^{2}}}\left(\frac{\partial \overline{w'^{2}}}{\partial t} + \frac{\partial \overline{w'^{3}}}{\partial z} - C_{0}\varepsilon\right) - \overline{w'^{2}}\frac{\partial \overline{w'^{2}}}{\partial z}}{\overline{w'^{4}} - \frac{\left(\overline{w'^{3}}\right)^{2}}{\overline{w'^{2}}} - \left(\overline{w'^{2}}\right)^{2}},$$

$$a_{1} = \frac{1}{2\overline{w'^{2}}}\left(\frac{\partial \overline{w'^{2}}}{\partial t} + \frac{\partial \overline{w'^{3}}}{\partial z} - C_{0}\varepsilon - 2\overline{w'^{3}}a_{2}\right),$$

$$a_{0} = \frac{\partial \overline{w'^{2}}}{\partial z} - \overline{w'^{2}}a_{2}.$$

Higher-order moments of the vertical velocity distribution $\overline{w'^3}$ and $\overline{w'^4}$ are determined from the vertical velocity variance using

$$\overline{w'^3} = 0.8 \left(\max \left(0, \overline{w'^2} - \overline{w_1'^2} \right) \right)^{3/2},$$

$$\overline{w'^4} = 3.5 \left(\overline{w'^2} \right)^2,$$

in the convective boundary layer, and Gaussian values elsewhere

$$\overline{w'^3} = 0.0,$$
 $\overline{w'^4} = 3.0 (\overline{w'^2})^2.$

The subscript 1 here refers to the value of this variable at the first model level (10 m). This parameterisation produces a skewness of zero at the bottom and top of the convective boundary layer, and a peak value of about 0.6 within this layer. These parameterisations agree with measurements in the convective boundary layer as discussed by Luhar et al. (1996).

The perturbation of vertical velocity due to plume rise effects is determined using a random walk approach

$$\dot{\sigma}'_{p} = (w_{p} + \xi \sigma_{wp}) \frac{\partial \sigma}{\partial z},$$

where ξ is a random number from a Gaussian distribution with mean zero and variance one, and plume rise variables w_p and σ_{wp} are defined in Section 3.3.

In order to calculate total pollutant concentration for use in chemistry calculations and timeaveraging, particles are converted to concentration at grid points of the EGM using the equation for the concentration increment of a particle at a grid point

$$\Delta \chi = \frac{\Delta m}{2\pi_c \sigma_v^2 \Delta z} \exp\left(-\frac{r^2}{2\sigma_v^2}\right),$$

where

 Δm is the particle mass,

 σ_{v} is the standard deviation of horizontal puff width,

 Δz is the vertical grid spacing,

r is the horizontal distance from the particle position to the grid point.

3.2.2 Chemistry

In tracer mode, optional chemical decay of a particular pollutant is represented by exponentially decaying particle mass. In chemistry mode, pollutant emissions are converted to particle mass on release from the source, and stored for the variables APM, FPM, SO_2 , NO_X , R_{smog} , SP_X and NO_2 . Chemistry is accounted for in these variables by the EGM. This approach allows the dispersion of the primary emissions of the above variables to be handled with the LPM, and avoids any dependence of the LPM on the EGM.

The diagnostic solution for the total concentration is then

$$\begin{split} [APM] &= [APM]_{LPM} + [APM]_{EGM} \,, \\ [FPM] &= [FPM]_{LPM} + [FPM]_{EGM} \,, \\ [SO_2] &= [SO_2]_{LPM} + [SO_2]_{EGM} \,, \\ [NO_X] &= [NO_X]_{LPM} + [NO_X]_{EGM} \,, \\ [R_{smog}] &= [R_{smog}]_{LPM} + [R_{smog}]_{EGM} \,, \\ [SP_X] &= [SP_X]_{LPM} + [SP_X]_{EGM} \,, \\ [NO_2] &= [NO_2]_{LPM} + [NO_2]_{EGM} \,, \\ [RP] &= [RP]_{EGM} \,, \\ [H_2O_2] &= [H_2O_2]_{EGM} \,. \end{split}$$

3.3 Plume rise module

The equations for mean plume rise of a point source emission are based on a simplified version of the model of Glendening et al. (1984)

$$\frac{dG}{dt} = 2R(\alpha w_p^2 + \beta u_a w_p),$$

$$\frac{dF}{dt} = -\frac{sM}{u_p} \left(\frac{M}{M_{eff}} u_a + w_p \right),$$

$$\frac{dM}{dt} = F,$$

$$\frac{dx_p}{dt} = u,$$

$$\frac{dy_p}{dt} = v,$$

$$\frac{dz_p}{dt} = w_p,$$

with

$$G = \frac{T_a}{T_p} u_p R^2,$$

$$F = g u_p R^2 \left(1 - \frac{T_a}{T_p} \right),$$

$$M = \frac{T_a}{T_p} u_p R^2 w_p,$$

$$w_p = \frac{M}{G},$$

$$R = \sqrt{\frac{(G+F/g)}{u_p}},$$

$$u_p = \sqrt{u_a^2 + w_p^2},$$

$$u_a = \sqrt{u^2 + v^2},$$

G, F, M = plume volume, buoyancy, and momentum flux respectively,

R =plume radius (top - hat cross - section),

u, v, w =cartesian x, y, z components of velocity respectively,

T = temperature,

s = ambient buoyancy frequency,

subscript a refers to ambient variables, subscript p refers to plume variables,

 α = 0.1, β = 0.6, are vertical plume and bent - over plume entrainment constants respectively, $\frac{M}{M_{eff}} = \frac{1}{2.25}$, g = gravitational constant (9.8 m s⁻²).

Initial conditions for these equations are

$$G_o = \frac{T_a}{T_s} w_s R_s^2$$
, $F_o = N_E g w_s R_s^2 \left(1 - \frac{T_a}{T_s}\right)$, $M_o = \frac{T_a}{T_s} w_s^2 R_s^2$, $R_o = R_s \sqrt{\frac{w_s}{\sqrt{u_a^2 + w_s^2}}}$,

where N_E is the user-specified buoyancy enhancement factor (e.g., see Manins et al., 1992, for parameterisations of N_E to handle overlapping plumes from multiple stacks), and subscript s representing stack exit conditions. Stack height is adjusted for stack-tip downwash following Briggs (1973), but with the restriction that this equation is not used for squat stacks (Hibberd, 2006, personal communication)

$$h_{sd} = \begin{cases} h_s - 4R_s \max(0, 1.5 - \frac{w_s}{u_a}), & \text{if } h_s > 10R_s \\ h_s, & \text{otherwise} \end{cases}$$

Plume rise is terminated when the plume dissipation rate decreases to ambient levels.

Tests of these equations against both the full Glendening and the Briggs (1975) form of the plume rise equations showed that the above approach was just as good as the full Glendening

form for all conditions. It also collapses to the Briggs form for a bent-over Boussinesq plume, and to the Briggs vertical plume model equations for zero ambient wind. For very hot plumes in a bent-over plume situation, the Briggs form was very close to our form, even though the Boussinesq approximation was not strictly valid. This finding is probably due to the rapid decrease of plume temperature excess with travel time.

In the EGM, plume rise for a point source is accounted for by releasing pollutants at the effective source height as calculated by the above equations, with a plume depth that assumes a 2:1 horizontal to vertical plume shape, and that the plume radius for concentration is two-thirds that of the visual radius R above. Pollutant emissions are then distributed uniformly to grid points within the plume depth at the nearest horizontal grid point (assuming plume width is always sub-grid scale).

In the LPM, a gradual plume rise approach is used with a random component that depends on the standard deviation of the vertical velocity due to plume rise effects, and an enhanced horizontal spread. The standard deviations of velocity assume a slightly simplified form of the above equation for G, a 2:1 horizontal to vertical plume shape, a plume radius for concentration of two-thirds the visual radius R, and a standard deviation half that of the radius. This results in the equations

$$\sigma_{wp} = \frac{\alpha w_p^2 + \beta u_a w_p}{3\sqrt{2}u_p}$$
, and $\sigma_{up} = 2\sigma_{wp}$.

3.4 Building wake module

The effect of building wakes on plume rise and dispersion is based on the Plume Rise Model Enhancements (PRIME) approach of Schulman et al. (2000). The PRIME model uses an along-wind coordinate system, and so first each building is transformed to be in this system. Effective building dimensions and cavity and wake dimensions are then calculated for each building and are then used to determine the combined wake meteorology and turbulence. Plume rise is affected by the modified meteorology and turbulence for point sources in both EGM and LPM modes, while dispersion is influenced only for plumes in LPM mode. LPM calculations are done for both the cavity and wake regions, rather than specifying a uniform concentration in the cavity as is done in PRIME.

3.4.1 Transformation to along-wind coordinate system

Using the local horizontal wind components (u, v) in a Cartesian coordinate system, a point (x, y) can be rotated to be in an along-wind coordinate system (x', y') by using the transformation

$$x' = (xu - yv)/U$$
 and $y' = (yu - xv)/U$, with $U = \sqrt{u^2 + v^2}$.

The horizontal coordinates of the building corners are converted to be in the along-wind coordinate system, using the above transformation. Then, after calculating the minimum and maximum corner point coordinate components, the effective building dimensions are calculated as length $L = x'_{\text{max}} - x'_{\text{min}}$ and width $W = y'_{\text{max}} - y'_{\text{min}}$. We then define the origin for this building at the centre of the upwind face of the building $(x'_0, y'_0) = (x'_{\text{min}}, \frac{1}{2}(y'_{\text{min}} + y'_{\text{max}}))$.

3.4.2 Building wake dimensions

Given an effective building length (L), width (W) and height (H) in an along-wind coordinate system (x, y, z) (m) with origin at the centre of the up-wind face of the building, a diffusion length scale (R) is

$$R = B_S^{2/3} B_L^{1/3}$$
, with $B_S = \min(H, W)$ and $B_L = \min(8B_S, \max(H, W))$.

The maximum height of the cavity (recirculation zone) is then

$$H_R = \begin{cases} H, & \text{if } L > 0.9R \text{ (reattachment)} \\ H + 0.22R, & \text{otherwise} \end{cases}$$

and the length of the cavity from the lee-face of the building is

$$L_{R} = \frac{1.8W}{\left(\max\left(0.3, \min\left(\frac{L}{H}, 3\right)\right)\right)^{0.3} \left(1 + 0.24 \frac{W}{H}\right)}.$$

The cavity height is

The cavity height is
$$\begin{cases}
H, & \text{if } 0 < x \le L \\
H\left(1 - \left(\frac{x - L}{L_R}\right)^2\right), & \text{if } L < x < L + L_R
\end{cases}, & \text{if } L > 0.9R
\end{cases}$$

$$H_C(x) = \begin{cases}
H_R + \frac{4(x - 0.5R)^2(H - H_R)}{R^2}, & \text{if } 0 < x \le 0.5R \\
H_R\left(1 - \frac{(x - 0.5R)^2}{(L + L_R - 0.5R)^2}\right)^{0.5}, & \text{if } 0.5R < x < L + L_R
\end{cases}, & \text{otherwise}$$

and the cavity width is

$$W_{C}(x) = \begin{cases} \frac{W}{2} + \frac{R}{3} - \frac{(x-R)^{2}}{3R}, & \text{if } 0 < x \le R \\ \left(\frac{W}{2} + \frac{R}{3}\right) \sqrt{1 - \left(\frac{x-R}{L+L_{R}}\right)^{2}}, & \text{if } R < x < L+L_{R} \end{cases}.$$

The wake height is

$$H_W(x) = 1.2R \left(\frac{x}{R} + \left(\frac{H}{1.2R}\right)^3\right)^{1/3}$$

and the wake width is

$$W_W(x) = \frac{W}{2} + \frac{R}{3} \left(\frac{x}{R}\right)^{1/3}$$
.

3.4.3 Building wake meteorology and turbulence

The meteorology and turbulence characteristics described below are used in the calculation of concentration in the following Sections.

Streamline slope over a building is calculated in along-wind coordinates as

$$\left(\frac{dz}{dx}\right)_{wake}(x) = \begin{cases}
0, & \text{if } x < -R \\
\frac{F_z 2(H_R - H)(x + R)}{R^2}, & \text{if } -R \le x < 0 \\
\frac{F_z 4(H_R - H)(R - 2x)}{R^2}, & \text{if } 0 \le x < 0.5R \\
\frac{F_z (H_R - H)(R - 2x)}{(L + L_R - 0.5R)^2} \left(\frac{z}{H}\right)^{0.3}, & \text{if } 0.5R \le x < L + L_R \\
\frac{F_z (H_R - H)(R - 2(L + L_R))}{(L + L_R - 0.5R)^2} \left(\frac{z}{H}\right)^{0.3} \left(\frac{L + L_R}{x}\right), & \text{if } x \ge L + L_R
\end{cases}$$

with $F_z = 1$ if $z \le H$, and if z > H then

$$F_z = \begin{cases} 1, & \text{if } x < -R \\ \left(\frac{H}{z}\right)^3, & \text{if } -R \le x < 0.5R. \\ \left(\frac{H}{z}\right), & \text{if } x \ge R \end{cases}$$

The horizontal wind speed factor F_U and the turbulence intensities i_x and i_z are calculated as follows

If
$$x \le L + L_R$$
 and $z \le H_R$

$$F_{U} = F_{C}$$

$$\begin{split} F_C &= \max \Biggl(0.1, 1 - \frac{\frac{\Delta U}{U} H_W}{0.5 \bigl(H_C + H_W \bigr)} \biggr), \\ i_z &= i_{zc} / \bigl(1 - \frac{\Delta U}{U} \bigr), \end{split}$$

$$i_x = 0.5 \max(0.3, \min(\frac{W}{H}, 3)),$$

otherwise if $z \le H_w$

$$F_{U} = F_{C} + (1 - F_{C}) \frac{(z - H_{C})}{(H_{W} - H_{C})},$$

$$F_{C} = \max \left(0.1, 1 - \frac{F_{x} \frac{\Delta U}{U} H_{W}}{0.5(H_{C} + H_{W})}\right),$$

$$i_{z} = 1.7i_{zN} \left(\frac{F_{x}}{1 - F_{x} \frac{\Delta U}{U}} \right),$$

$$i_{x} = i_{z},$$

$$F_{x} = \begin{cases} \left(\frac{x}{L} \right)^{2/3}, & \text{if } 0 < x < L \\ \left(\frac{R}{x - L + R} \right)^{2/3}, & \text{if } x \ge L \end{cases}$$

with
$$\frac{\Delta U}{U} = 0.7$$
, $i_{zc} = 0.65$ and $i_{zN} = 0.06$.

Note that we have parameterised cavity turbulence, and do not assume a uniform cavity concentration as is done in PRIME. Note also that wake calculations are done only if x < 15R and $|y| < 0.5W_w$.

3.4.4 Treatment of multiple building blocks

If we define a building block as having a constant height H, then we can use the above procedure to define wake characteristics for each building block. The effects of overlapping wakes from multiple building blocks, whether from the same multi-level or multi-tiered physical building, or from multiple physical buildings, can be treated by combining the meteorology and turbulence. For a particular point in space, the combined (for all building blocks)

- streamline slope can be calculated by first calculating the maximum slope and the
 minimum slope, and then if the absolute value of the maximum is greater than the
 absolute value of the minimum, then use the maximum value, otherwise use the
 minimum value;
- horizontal wind speed factor is the minimum value;
- turbulence intensity is the maximum value.

The combined effects can then be used for the calculation of plume rise and dispersion – the above approach attempts to be conservative for expected ground-level pollution concentration.

3.4.5 Wake effects on plume rise

For the calculation of plume rise (Section 3.3), the horizontal wind and the differential equations for G and z_p are adjusted as follows

$$u = u_{old} F_U$$
, $v = v_{old} F_U$ and then $U = \sqrt{u^2 + v^2}$,

$$\frac{dG}{dt} = \max\left(\frac{dG}{dt}\bigg|_{old}, \sqrt{\frac{\pi_c}{2}}U^2 i_z\right),\,$$

$$\frac{dz_p}{dt} = \frac{dz_p}{dt}\bigg|_{old} + U\bigg(\frac{dz}{dx}\bigg)_{wake}.$$

3.4.6 Wake effects on LPM dispersion

For LPM dispersion, the mean wind is modified

$$u = u_{old} F_U$$
, $v = v_{old} F_U$ and then $U = \sqrt{u^2 + v^2}$, and $w = w_{old} + U \left(\frac{dz}{dx}\right)_{wake}$,

while the horizontal plume spread incorporates an extra term using $\sigma_u = Ui_x$ and the LPM random-walk equation also includes a contribution from $\sigma_w = Ui_z$.

3.4.7 Wake effects on EGM dispersion

The influence of building wakes on dispersion in EGM mode allows them to be included not only for point sources, but also for line, area/volume and gridded emission sources. The approach taken is to modify the mean and turbulence fields from those predicted with the meteorological module, by using the same corrections for building wake meteorology and turbulence as above, based on the PRIME parameterisations.

For EGM dispersion, the mean wind is modified

$$u = u_{old} F_U$$
, $v = v_{old} F_U$ and then $U = \sqrt{u^2 + v^2}$, and $w = w_{old} + U \left(\frac{dz}{dx}\right)_{wake}$,

while the turbulence is modified

$$E = E_{old} + E_{wake}$$

$$\boldsymbol{\varepsilon} = \boldsymbol{\varepsilon}_{old} + \boldsymbol{\varepsilon}_{wake}$$

with

$$\begin{split} E_{wake} &\equiv \sigma_u^2 + \frac{1}{2}\sigma_w^2 = \left(Ui_x\right)^2 + \frac{1}{2}\left(Ui_z\right)^2 \\ \varepsilon_{wake} &= c_m^{3/4} \, \frac{E_{wake}^{3/2}}{H} \end{split}$$

Note that here the value of H_w is the maximum of the building wake heights at a particular point, when there are multiple buildings. The diffusion coefficient is calculated using E and ε above, using the standard definition.

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4 Numerical methods

The flow chart in Figure 1 illustrates the order of calculations in the model. The model uses a large timestep of 300 s on which radiation and surface processes are calculated. Meteorological and turbulence equations are solved with a timestep of $\Delta t_M = \frac{1}{U_M} \min(\Delta x_M, \Delta y_M)$, where U_M is a characteristic tropospheric wind speed $(U_M = 40 \text{ m s}^{-1} \text{ is the model default})$, and Δx_M and Δy_M are the horizontal grid spacings in metres on the meteorological grid. A cap on the meteorological advection and diffusion timestep is set at 150 s to aid stability for larger grid spacing. Pollution concentration equations for the EGM are solved with a timestep of $\Delta t_P = \frac{1}{U_P} \min(\Delta x_P, \Delta y_P)$, where $U_P = 0.5 U_M$, and Δx_P and Δy_P are the horizontal grid spacings in metres on the pollution grid. The pollution grid can be a subset of the meteorological grid at finer grid spacing.

Model equations are solved using finite difference methods with no grid stagger, a constant grid spacing in the horizontal directions, and a variable grid spacing in the vertical direction. Second-order centred spatial differencing is used, for example

$$\begin{split} \frac{\partial \phi}{\partial x}\bigg|_{i} &= \frac{1}{2\Delta x} \left(\phi_{i+1} - \phi_{i-1}\right), \\ \frac{\partial \phi}{\partial y}\bigg|_{j} &= \frac{1}{2\Delta y} \left(\phi_{j+1} - \phi_{j-1}\right), \\ \frac{\partial \phi}{\partial \sigma}\bigg|_{k} &= \frac{1}{(\sigma_{k+1} - \sigma_{k-1})} \left(\left(\frac{\sigma_{k} - \sigma_{k-1}}{\sigma_{k+1} - \sigma_{k}}\right) \left(\phi_{k+1} - \phi_{k}\right) + \left(\frac{\sigma_{k+1} - \sigma_{k}}{\sigma_{k} - \sigma_{k-1}}\right) \left(\phi_{k} - \phi_{k-1}\right)\right), \\ \frac{\partial}{\partial x} \left(K \frac{\partial \phi}{\partial x}\right)\bigg|_{i} &= \frac{1}{2(\Delta x)^{2}} \left(\left(K_{i+1} + K_{i}\right) \left(\phi_{i+1} - \phi_{i}\right) - \left(K_{i} + K_{i-1}\right) \left(\phi_{i} - \phi_{i-1}\right)\right), \\ \frac{\partial}{\partial y} \left(K \frac{\partial \phi}{\partial y}\right)\bigg|_{j} &= \frac{1}{2(\Delta y)^{2}} \left(\left(K_{j+1} + K_{j}\right) \left(\phi_{j+1} - \phi_{j}\right) - \left(K_{j} + K_{j-1}\right) \left(\phi_{j} - \phi_{j-1}\right)\right), \\ \frac{\partial}{\partial \sigma} \left(K \frac{\partial \phi}{\partial \sigma}\right)\bigg|_{k} &= \frac{1}{(\sigma_{k+1} - \sigma_{k-1})} \left(\left(\frac{K_{k+1} + K_{k}}{\sigma_{k+1} - \sigma_{k}}\right) \left(\phi_{k+1} - \phi_{k}\right) - \left(\frac{K_{k} + K_{k-1}}{\sigma_{k} - \sigma_{k-1}}\right) \left(\phi_{k} - \phi_{k-1}\right)\right). \end{split}$$

4.1 Horizontal advection

Horizontal advection for all prognostic variables is calculated with timesteps Δt_M or Δt_P using the semi-Lagrangian technique of McGregor (1993) with the quasi-monotone conversion of Bermejo and Staniforth (1992). To $O((\Delta t)^2)$, the departure point (i_*, j_*) in grid units can be determined for horizontal grid point (i, j) from

$$i_* = i - u_{i,j}^{n+1/2} \frac{\Delta t}{\Delta x} + \frac{(\Delta t)^2}{2\Delta x} \left(u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} \right) \Big|_{i,j}^{n+1/2},$$

$$j_* = j - v_{i,j}^{n+1/2} \frac{\Delta t}{\Delta y} + \frac{(\Delta t)^2}{2\Delta y} \left(u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} \right) \Big|_{i,j}^{n+1/2},$$

with $u_{i,j}^{n+1/2} = 1.5u_{i,j}^n - 0.5u_{i,j}^{n-1}$ or $u_{i,j}^{n+f} = fu_{i,j}^{n+1} + (1-f)u_{i,j}^n$ and similarly for v, for the meteorological and concentration variables respectively (f accounts for fractional timesteps). Each prognostic variable can then be determined from $\phi_{i,j}^{n+1} = \phi_{i_*,j_*}^n$ using Lagrange cubic polynomial interpolation separately in each coordinate direction.

Defining
$$i = \text{int}(i_*)$$
 and $x_* = i_* - i$, then $\phi_{i_*j}^n = -\frac{1}{6}x_*(x_* - 1)(x_* - 2)\phi_{i-1j}^n + \frac{1}{2}(x_*^2 - 1)(x_* - 2)\phi_{ij}^n - \frac{1}{2}x_*(x_* + 1)(x_* - 2)\phi_{i+1j}^n + \frac{1}{6}x_*(x_*^2 - 1)\phi_{i+2j}^n$, subject to $\min(\phi_{ij}^n, \phi_{i+1j}^n) \le \phi_{i_*j}^n \le \max(\phi_{ij}^n, \phi_{i+1j}^n)$. Similarly, if $j = \text{int}(j_*)$ and $y_* = j_* - j$, then $\phi_{i_*j_*}^n = -\frac{1}{6}y_*(y_* - 1)(y_* - 2)\phi_{i_*j-1}^n + \frac{1}{2}(y_*^2 - 1)(y_* - 2)\phi_{i_*j+2}^n + \frac{1}{6}y_*(y_*^2 - 1)\phi_{i_*j+2}^n$, subject to $\min(\phi_{i_*j}^n, \phi_{i_*j+1}^n) \le \phi_{i_*j_*}^n \le \max(\phi_{i_*j}^n, \phi_{i_*j+1}^n)$.

4.2 Vertical advection

Vertical advection for all prognostic variables except θ_{ν} , is calculated with timesteps Δt_M or Δt_P using the semi-Lagrangian technique of McGregor (1993) with the quasi-monotone conversion of Bermejo and Staniforth (1992). To $O((\Delta t)^2)$, the departure point can be determined from

$$\sigma_* = \sigma_k - \dot{\sigma}_k^{n+1/2} \Delta t + \frac{1}{2} (\Delta t)^2 \left(\dot{\sigma} \frac{\partial \dot{\sigma}}{\partial \sigma} \right) \Big|_k^{n+1/2},$$

with $\dot{\sigma}_k^{n+1/2} = 1.5 \dot{\sigma}_k^n - 0.5 \dot{\sigma}_k^{n-1}$ or $\dot{\sigma}_k^{n+f} = f \dot{\sigma}_k^{n+1} + (1-f) \dot{\sigma}_k^n$, for the meteorological and concentration variables respectively (f accounts for fractional timesteps). Each prognostic variable can then be determined from $\phi_k^{n+1} = \phi_{k_*}^n$ (where k denotes the nearest model level to σ_* that satisfies $\sigma_k \leq \sigma_*$), using Lagrange cubic polynomial interpolation (with quasi-monotone conversion)

$$\begin{split} \phi_{k_*}^n &= \left(\frac{\sigma_* - \sigma_k}{\sigma_{k-1} - \sigma_k}\right) \left(\frac{\sigma_* - \sigma_{k+1}}{\sigma_{k-1} - \sigma_{k+1}}\right) \left(\frac{\sigma_* - \sigma_{k+2}}{\sigma_{k-1} - \sigma_{k+2}}\right) \phi_{k-1}^n \\ &+ \left(\frac{\sigma_* - \sigma_{k-1}}{\sigma_k - \sigma_{k-1}}\right) \left(\frac{\sigma_* - \sigma_{k+1}}{\sigma_k - \sigma_{k+1}}\right) \left(\frac{\sigma_* - \sigma_{k+2}}{\sigma_k - \sigma_{k+2}}\right) \phi_k^n \\ &+ \left(\frac{\sigma_* - \sigma_{k-1}}{\sigma_{k+1} - \sigma_{k-1}}\right) \left(\frac{\sigma_* - \sigma_k}{\sigma_{k+1} - \sigma_k}\right) \left(\frac{\sigma_* - \sigma_{k+2}}{\sigma_{k+1} - \sigma_{k+2}}\right) \phi_{k+1}^n \\ &+ \left(\frac{\sigma_* - \sigma_{k-1}}{\sigma_{k+2} - \sigma_{k-1}}\right) \left(\frac{\sigma_* - \sigma_k}{\sigma_{k+2} - \sigma_k}\right) \left(\frac{\sigma_* - \sigma_{k+1}}{\sigma_{k+2} - \sigma_{k+1}}\right) \phi_{k+2}^n, \end{split}$$

subject to $\min(\phi_k^n, \phi_{k+1}^n) \le \phi_{k}^n \le \max(\phi_k^n, \phi_{k+1}^n)$.

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Start Nesting Loop					
Initialisation					
Start Main Time Loop ($\Delta t = 300 \text{ s}$)					
Update Surface Temperature, Surface Fluxes and Radiation					
Start Meteorological Time Loop (Δt_M)					
Semi-Lagrangian Advection					
Update Microphysics					
Start Gravity Wave Time Loop (Δt _G)					
Update Velocity, Potential Virtual Temperature and Hydrostatic Exner Pressure Function					
End Gravity Wave Time Loop					
Update Non-Hydrostatic Exner Pressure Function					
Update Specific Humidities of Water Vapour, Cloud Water and Rain Water					
Update Turbulence Kinetic Energy, Eddy Dissipation Rate and Eddy Diffusivity					
End Meteorological Time Loop					
Interpolation of Meteorological Variables to the Pollution Grid					
Plume Rise Module and Building Wake Module					
Lagrangian Particle Module (LPM)					
Start Pollution (EGM) Time Loop (Δt _P)					
Semi-Lagrangian Advection					
Update Pollutant Concentrations					
End Pollution Time Loop					
End Main Time Loop					
Output					
End Nesting Loop					

Figure 1. Flow chart of TAPM. © CSIRO 2008

4.3 Gravity waves

The equations for the meteorological variables $u, v, \dot{\sigma}, \theta_v$, and π_H are solved by using a time-split approach where gravity wave terms are separated from the others and solved on a small timestep $\Delta t_G = \frac{1}{U_G} \min(\Delta x_M, \Delta y_M)$, where $U_G = 160 \text{ m s}^{-1}$

$$\begin{split} \frac{\partial u}{\partial t} &= -\theta_{v} \, \frac{\partial \pi_{H}}{\partial x} + R_{u} \,, \\ \frac{\partial v}{\partial t} &= -\theta_{v} \, \frac{\partial \pi_{H}}{\partial y} + R_{v} \,, \\ \frac{\partial \dot{\sigma}}{\partial \sigma} &= -\bigg(\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \bigg) + u \, \frac{\partial^{2} \sigma}{\partial \sigma \partial x} + v \, \frac{\partial^{2} \sigma}{\partial \sigma \partial y} \,, \\ \frac{\partial \theta_{v}}{\partial t} &= -\dot{\sigma} \, \frac{\partial \theta_{v}}{\partial \sigma} + R_{\theta_{v}} \,, \\ \frac{\partial \pi_{H}}{\partial \sigma} &= -\frac{g}{\theta_{v}} \bigg(\frac{\partial \sigma}{\partial z} \bigg)^{-1} \,, \end{split}$$

with R_u , R_v , and R_{θ_u} (updated on the timestep Δt_M)

$$\begin{split} R_{u} &= g \, \frac{\partial \sigma}{\partial x} \bigg(\frac{\partial \sigma}{\partial z} \bigg)^{-1} + f(v - v_{s}) - N_{s} \big(u - u_{s} \big) - \theta_{v} \bigg(\frac{\partial \pi_{N}}{\partial x} + \frac{\partial \pi_{N}}{\partial \sigma} \frac{\partial \sigma}{\partial x} \bigg), \\ R_{v} &= g \, \frac{\partial \sigma}{\partial y} \bigg(\frac{\partial \sigma}{\partial z} \bigg)^{-1} - f(u - u_{s}) - N_{s} \big(v - v_{s} \big) - \theta_{v} \bigg(\frac{\partial \pi_{N}}{\partial y} + \frac{\partial \pi_{N}}{\partial \sigma} \frac{\partial \sigma}{\partial y} \bigg), \\ R_{\theta_{v}} &= S_{\theta_{v}} - \gamma_{cg} \, \frac{\partial K}{\partial \sigma} \frac{\partial \sigma}{\partial z} - N_{s} \big(\theta_{v} - \theta_{vs} \big), \end{split}$$

and also include the nesting terms.

These prognostic equations are solved using the second-order Adams-Bashforth scheme

$$u^{n+1} = u^n + \frac{\Delta t}{2} \left(3 \frac{\partial u}{\partial t} \bigg|^n - \frac{\partial u}{\partial t} \bigg|^{n-1} \right),$$

while diagnostic vertical integration using the trapezoidal rule is performed from the ground to the model top to obtain $\dot{\sigma}$, and from the model top to the ground to obtain π_H .

On the timestep Δt_G , an implicit tri-diagonal horizontal filter described by Pielke (2002) is used. The filter, represented by $F(\phi)$ in equations 1, 2 and 4 of Section 2.1, is applied separately in each horizontal direction with a filter coefficient of $\delta = 0.10$ (increased values are used near the top of the model). The equations solved are

$$(1-\delta)\phi_{i-1j}^{n+1} + 2(1+\delta)\phi_{ij}^{n+1} + (1-\delta)\phi_{i+1j}^{n+1} = \phi_{i-1j}^{n} + 2\phi_{ij}^{n} + \phi_{i+1j}^{n},$$

$$(1-\delta)\phi_{ii-1}^{n+1} + 2(1+\delta)\phi_{ii}^{n+1} + (1-\delta)\phi_{ii+1}^{n+1} = \phi_{ii-1}^{n} + 2\phi_{ii}^{n} + \phi_{ii+1}^{n}.$$

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On the timestep Δt_M , vertical diffusion is solved using a first-order implicit approach with special treatment of fluxes at the surface boundary (see next section).

4.4 Scalar prognostic equations

All other prognostic equations including those for specific humidity, turbulence, and pollutant concentrations, are of the general form for variable χ

$$\frac{\partial \chi}{\partial t} = \left(\frac{\partial \sigma}{\partial z}\right)^2 \frac{\partial}{\partial \sigma} \left(K \frac{\partial \chi}{\partial \sigma}\right) + RHS_1 - \chi RHS_2.$$

This equation is solved using first-order time differencing with a semi-implicit approach to give the equation

$$(1 + \Delta t R H S_2) \chi^{n+1} - \Delta t \left(\frac{\partial \sigma}{\partial z} \right)^2 \frac{\partial}{\partial \sigma} \left(K \frac{\partial \chi^{n+1}}{\partial \sigma} \right) = \chi^n + \Delta t R H S_1,$$

which can be solved as follows (with special treatment of fluxes at the surface) using a tridiagonal solution method if second-order spatial differencing is used

$$A\chi_{k-1}^{n+1} + B\chi_k^{n+1} + C\chi_{k+1}^{n+1} = D;$$

if k > 1:

$$A = -\left(\frac{\partial \sigma}{\partial z}\right)^{2} \frac{\Delta t}{\left(\sigma_{k+1} - \sigma_{k-1}\right)} \left(\frac{K_{k} + K_{k-1}}{\sigma_{k} - \sigma_{k-1}}\right),$$

$$C = -\left(\frac{\partial \sigma}{\partial z}\right)^{2} \frac{\Delta t}{\left(\sigma_{k+1} - \sigma_{k-1}\right)} \left(\frac{K_{k+1} + K_{k}}{\sigma_{k+1} - \sigma_{k}}\right),$$

$$B = 1 + \Delta t R H S_2 - A - C,$$

$$D = \chi_k^n + \Delta t R H S_1;$$

if
$$k = 1$$
:

$$A = 0$$
,

$$C = -\frac{1}{2} \left(\frac{\partial \sigma}{\partial z} \right)^2 \frac{\Delta t}{\left(\sigma_{3/2} - \sigma_0 \right)} \left(\frac{K_2 + K_1}{\sigma_2 - \sigma_1} \right),$$

$$B = 1 + \Delta t R H S_2 - C,$$

$$D = \chi_1^n + \Delta t RHS_1 - \Delta t \left(\frac{\partial \sigma}{\partial z}\right) \frac{\text{flux}(\chi)}{\left(\sigma_{3/2} - \sigma_0\right)},$$

with flux(
$$\chi$$
) = $u_*\chi_*$ or flux(χ) = $V_d\chi_1$.

The value of RHS_2 is non-zero only for the ε equation, and the SO₂, NO₂, RP and H₂O₂ pollutant concentration equations, where the loss terms are treated implicitly. The RHS_1 term includes all other terms in the particular prognostic equations, including explicit horizontal diffusion. The non-zero RHS_2 terms are

$$\begin{split} \varepsilon: RHS_2 &= c_{\varepsilon^2} \frac{\mathcal{E}}{E}, \\ [SO_2]: RHS_2 &= k_8[RP] + k_9[H_2O_2] + k_{10}[O_3], \\ [NO_2]: RHS_2 &= k_3 + k_4 \big([NO_X] + [SP_X] - [NO_2] \big), \\ [RP]: RHS_2 &= k_2[NO] + k_5[RP] + (k_6 + k_7)[NO_2] + k_8[SO_2], \\ [H_2O_2]: RHS_2 &= k_9[SO_2]. \end{split}$$

4.5 Other methods

- On the timestep Δt_M , the elliptic non-hydrostatic pressure perturbation equation is solved using an iterative approach. The solution is performed only for a sub-grid region that excludes the 5 edge grid points at the top and lateral boundaries, as these edge regions usually contain noisy solutions which can produce spurious vertical velocities to which the non-hydrostatic solution is highly sensitive.
- For numerical representation of the vertical fluxes, it is necessary to use a finite difference approximation consistent with that used for the vertical diffusion

$$\begin{split} \overline{w'\chi'}\Big|_{k} &= -\frac{1}{2}(K_{k+1} + K_{k}) \left(\frac{\sigma_{k} - \sigma_{k-1}}{\sigma_{k+1} - \sigma_{k-1}} \right) \left(\frac{\chi_{k+1} - \chi_{k}}{\sigma_{k+1} - \sigma_{k}} \right) \left(\frac{\partial \sigma}{\partial z} \right) \\ &- \frac{1}{2}(K_{k} + K_{k-1}) \left(\frac{\sigma_{k+1} - \sigma_{k}}{\sigma_{k+1} - \sigma_{k-1}} \right) \left(\frac{\chi_{k} - \chi_{k-1}}{\sigma_{k} - \sigma_{k-1}} \right) \left(\frac{\partial \sigma}{\partial z} \right). \end{split}$$

- At times of rapid variations in the surface temperature and specific humidity (such as just after sunrise), the surface heat balance approach used for vegetation can produce oscillations. Therefore, the vegetation temperature and moisture are time averaged using the current and previous values to prevent the oscillations.
- Linear interpolation is used to convert the synoptic-scale variables from the gridded analyses to the model.
- The plume rise equations are solved using the fourth-order Runge-Kutta method with a timestep of 1 second.
- The LPM uses explicit, forward in time finite differences and centred in space finite differences, with a large timestep of $\Delta t_{LPM} = 2\Delta t_P$ and a small timestep of 5 seconds for the solution in the vertical direction.
- The turbulence production/dissipation balance and wet processes are handled separately on a small timestep of 100 s.
- For multi-dimensional simulations, it was found necessary to bound the value of the length scale in order to keep the numerical solution stable for the ε prognostic equation. Also, the counter-gradient tracer flux and cross-correlation term are restricted to be zero in thermally stable regions, and are bounded elsewhere.

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Appendix

The following summarises non-default turbulence and land surface scheme options in TAPM.

Alternate Turbulence Schemes

The TAPM V3 turbulence closure options based on Hurley (1997) are as follows. The mean equations use a gradient diffusion approach, which depends on a diffusion coefficient K and gradients of mean variables. Using Cartesian tensor notation, the fluxes are

$$\overline{u_i'u_j'} = \frac{2}{3}E\delta_{ij} - K\left(\frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i}\right),$$

$$\overline{u_i'\theta_v'} = -K\left(\frac{\partial \theta_v}{\partial x_i} - \gamma_{\theta_v}\right),$$

$$\overline{u_i'\phi'} = -2.5K\frac{\partial \phi}{\partial x_i},$$

where

i, j are subscripts for the three coordinate directions (i.e. i = 1,2,3 for x,y,z respectively), u_i, u_j represent velocities,

$$\delta_{ij} = \begin{cases} 1 & \text{if } i = j, \\ 0 & \text{otherwise.} \end{cases}$$

 $\gamma_{\theta_{v}} = 0.00065 \text{ K m}^{-1} \text{ from Deardorff (1966)},$

 ϕ represents a scalar.

The scalar diffusion coefficient of 2.5 used above is based on an analysis of the second order closure equations from Andren (1990), with constants from Rodi (1985).

The turbulence scheme used to calculate K is the standard E- ε model in three-dimensional terrain-following coordinates, with constants for the eddy dissipation rate equation derived from the analysis of Duynkerke (1988). The model solves prognostic equations for the turbulence kinetic energy (E) and the eddy dissipation rate (ε)

$$\frac{dE}{dt} = \frac{\partial}{\partial x} \left(K_{H} \frac{\partial E}{\partial x} \right) + \frac{\partial}{\partial y} \left(K_{H} \frac{\partial E}{\partial y} \right) + \left(\frac{\partial \sigma}{\partial z} \right)^{2} \frac{\partial}{\partial \sigma} \left(K \frac{\partial E}{\partial \sigma} \right) + P_{s} + P_{b} - \varepsilon,$$

$$\frac{d\varepsilon}{dt} = \frac{\partial}{\partial x} \left(K_{H} \frac{\partial \varepsilon}{\partial x} \right) + \frac{\partial}{\partial y} \left(K_{H} \frac{\partial \varepsilon}{\partial y} \right) + \left(\frac{\partial \sigma}{\partial z} \right)^{2} \frac{\partial}{\partial \sigma} \left(c_{\varepsilon 0} K \frac{\partial \varepsilon}{\partial \sigma} \right)$$

$$+ \frac{\varepsilon}{E} (c_{\varepsilon 1} \max(P_{s}, P_{s} + P_{b}) - c_{\varepsilon 2} \varepsilon),$$

where

$$\begin{split} P_s &= 2K \Biggl(\Biggl(\frac{\partial u}{\partial x} + \frac{\partial u}{\partial \sigma} \frac{\partial \sigma}{\partial x} \Biggr)^2 + \Biggl(\frac{\partial v}{\partial y} + \frac{\partial v}{\partial \sigma} \frac{\partial \sigma}{\partial y} \Biggr)^2 + \Biggl(\frac{\partial w}{\partial \sigma} \frac{\partial \sigma}{\partial z} \Biggr)^2 \Biggr) \\ &+ K \Biggl(\Biggl(\frac{\partial u}{\partial y} + \frac{\partial u}{\partial \sigma} \frac{\partial \sigma}{\partial y} + \frac{\partial v}{\partial x} + \frac{\partial v}{\partial \sigma} \frac{\partial \sigma}{\partial x} \Biggr)^2 \Biggr) \\ &+ K \Biggl(\Biggl(\frac{\partial u}{\partial \sigma} \frac{\partial \sigma}{\partial z} + \frac{\partial w}{\partial x} + \frac{\partial w}{\partial \sigma} \frac{\partial \sigma}{\partial x} \Biggr)^2 + \Biggl(\frac{\partial v}{\partial \sigma} \frac{\partial \sigma}{\partial z} + \frac{\partial w}{\partial y} + \frac{\partial w}{\partial \sigma} \frac{\partial \sigma}{\partial y} \Biggr)^2 \Biggr), \\ P_b &= -\frac{g}{\theta_v} K \Biggl(\frac{\partial \theta_v}{\partial \sigma} \frac{\partial \sigma}{\partial z} - \gamma_{\theta_v} \Biggr), \\ \text{with } w &= \Biggl(\frac{\partial \sigma}{\partial z} \Biggr)^{-1} \Biggl(\mathring{\sigma} - u \frac{\partial \sigma}{\partial x} - v \frac{\partial \sigma}{\partial y} \Biggr), \\ \text{and } K_H &= \max(10, K), \ K = c_m \frac{E^2}{\varepsilon}, \ c_m = 0.09, \ c_{\varepsilon 0} = 0.69, \ c_{\varepsilon 1} = 1.46, \ \text{and} \ c_{\varepsilon 2} = 1.83. \end{split}$$

As an alternative to Equation (10) the model has an option to use a diagnostic eddy dissipation rate based on Duynkerke and Driedonks (1987). In this approach,

$$\begin{split} \varepsilon &= c_m^{3/4} \frac{E^{3/2}}{l}, \\ l &= \min(l_b, l_s), \\ l_b &= \left(\frac{\phi_M}{kz} + \frac{1}{l_o}\right)^{-1}, \\ l_s &= 0.36 E^{1/2} \left(\frac{g}{\theta_v} \frac{\partial \theta_v}{\partial z}\right)^{-1/2}, \\ l_o &= 0.3 \frac{\int Ez dz}{\int E dz}, \end{split}$$

 ϕ_M = surface layer similarity function (see Section 2.6.4),

k = von Karman constant (0.4).

Turbulence kinetic energy and eddy dissipation rate are enhanced in the top-half of the convective boundary layer (CBL), where turbulence levels can be underestimated using the above approaches. This has been achieved by using a simple parameterisation that limits the rate of decrease of prognostic turbulence with height, between heights in the range 0.55–0.95 times the CBL height, provided that the height is above the surface layer and the convective velocity scale is greater than 0.5 m s⁻¹.

In order to account for the neglect of some cloud processes (e.g. shallow convection), we enhance the synoptic total water used in the model, by enhancing the synoptic-scale specific humidity:

$$q_{enhanced} = \max(q_{synoptic}, 2q_{synoptic} - q_{sat}RH_C/100),$$

where $q_{synoptic}$ is the original synoptic-scale specific humidity and $RH_C = 85\%$ is the threshold value above which enhancement is carried out. This parameterisation results in no change to the synoptic-scale relative humidity for $RH_{synoptic} < RH_C$ and gives an enhanced value of 100% when $RH_{synoptic} = 92.5\%$. This approach is consistent with cloud cover parameterisations used in global and synoptic scale models.

Alternate Land Surface Schemes

The TAPM V3 land surface scheme to parameterise soil and vegetation effects are based on those from Kowalczyk et al. (1991), as described below.

Boundary conditions for mean variables at the surface are zero velocity, π_0 from the hydrostatic equation (5), $\theta_{v0} = c_p T_0 (1 + 0.61 q_0) / \pi_0$, with $T_0 = (1 - \sigma_f) T_g + \sigma_f T_f$ and $q_0 = (1 - \sigma_f) q_g + \sigma_f q_f$, where σ_f is the fraction of foliage cover and subscripts g and f denote soil and foliage respectively.

Note that if the surface type is water, then the surface temperature is set equal to the water surface temperature, and surface moisture is set equal to the saturation value. If the surface type is permanent ice/snow, then the surface temperature is set equal to -10° C, and surface moisture is set equal to the saturation value.

Soil parameterisation

Equations for soil temperature T_g , moisture content η_g and specific humidity q_g are

$$\begin{split} \frac{\partial T_g}{\partial t} &= \frac{3.72G_g}{\rho_s c_s d_1'} - \frac{7.4(T_g - T_d)}{24 \times 3600}, \\ \frac{\partial \eta_g}{\partial t} &= -\frac{c_1 \left(E_g (1 - \sigma_f) - \rho_w ((1 - \sigma_f) P + \sigma_f P_g - R) \right)}{\rho_w d_1} - \frac{c_2 (\eta_g - \eta_{eq})}{24 \times 3600}, \end{split}$$

$$q_g = f_{wet} q_0^* + (1 - f_{wet}) q_1,$$

where

$$G_g = R_{sw}^{in}(1 - \alpha_g) + R_{lw}^{in} - \sigma_{SB}T_g^4 \cos \alpha - H_g - \lambda E_g = \text{soil heat flux (W m}^{-2}),$$

$$H_g = \rho c_p (\theta_g - \theta_1) / r_H = \text{sensible heat flux (W m}^{-2}),$$

$$\lambda E_g = \rho \lambda (q_g - q_1) / r_H = \text{evaporative heat flux (W m}^{-2}),$$

 $r_{\rm H}$ is the aerodynamic resistance (see Section 2.6.4) with a roughness length of 0.1 m,

$$\eta_{\mathrm{eq}} = \eta_{\mathrm{d}} - \eta_{\mathrm{sat}} a_{\eta} \left(\frac{\eta_{\mathrm{d}}}{\eta_{\mathrm{sat}}} \right)^{b_{\eta}} \left(1 - \left(\frac{\eta_{\mathrm{d}}}{\eta_{\mathrm{sat}}} \right)^{8b_{\eta}} \right),$$

 T_d , η_d = deep soil temperature and moisture (model input),

$$\lambda = 2.5 \times 10^6 \text{ J kg}^{-1}, \ \rho_w = 1000 \text{ kg m}^{-3},$$

$$d_1' = \sqrt{\frac{k_s \times 24 \times 3600}{\rho_s c_s \pi_c}}, d_1 = 0.1,$$

 $\alpha_{\rm g}$, $k_{\rm s}$, $\rho_{\rm s}$, $c_{\rm s}$ = soil albedo, conductivity, density, and heat capacity, P, $P_{\rm g}$ = precipitation reaching the vegetation and soil respectively, $q_{\rm g}^*$ = soil saturated specific humidity, R = runoff.

The soil characteristics are specified for three soil types

$$k_{s} = 419(a_{s}\eta_{g} - b_{s}\eta_{g}^{0.4}),$$

$$\rho_{s}c_{s} = (1 - \eta_{sat})\rho_{s}^{dry}c_{s}^{dry} + \eta_{g}\rho_{w}c_{w},$$

$$c_{w} = 4186,$$

Sand:

$$c_1 = \begin{cases} 10 & \text{; for } \eta_r \le 0.05, \\ \frac{(1.8\eta_r + 0.962)}{(5.0\eta_r + 0.2)}; & \text{otherwise.} \end{cases}$$

$$c_2 = 2.0;$$

$$f_{wet} = \begin{cases} 1 & \text{; for } \eta_r \ge 0.15, \\ 11.49(\eta_r - 0.063); \text{ for } 0.063 \le \eta_r \le 0.15, \\ 0 & \text{; for } \eta_r < 0.063. \end{cases}$$

$$\eta_r = \eta_0 / \eta_{sat}, \eta_{sat} = 0.395, \eta_{wilt} = 0.068,$$
 $a_s = 0.004, b_s = 0.006, \rho_s^{dry} = 1600, c_s^{dry} = 800, a_\eta = 0.387, b_\eta = 4.$

Sandy Clay Loam:

$$c_1 = \begin{cases} 10 & \text{; for } \eta_r \le 0.226, \\ \frac{(1.78\eta_r + 0.253)}{(2.96\eta_r - 0.581)}; \text{ otherwise.} \end{cases}$$

$$c_2 = 3.0;$$

$$f_{wet} = \begin{cases} 1 & ; \text{for } \eta_r \ge 0.365, \\ 6.90(\eta_r - 0.22); \text{for } 0.22 \le \eta_r \le 0.365, \\ 0 & ; \text{for } \eta_r < 0.22. \end{cases}$$

$$\eta_r = \eta_0 / \eta_{sat}, \eta_{sat} = 0.420, \eta_{wilt} = 0.175,$$

$$a_s = 0.003, b_s = 0.004, \rho_s^{dry} = 1600, c_s^{dry} = 845, a_{\eta} = 0.135, b_{\eta} = 6.$$

Clay:

$$c_1 = \begin{cases} 10 & \text{; for } \eta_r \le 0.421, \\ \frac{(2.22\eta_r - 0.556)}{(2.78\eta_r - 1.114)}; & \text{otherwise.} \end{cases}$$

$$c_2 = 1.9$$
;

$$f_{wet} = \begin{cases} 1 & ; \text{for } \eta_r \ge 0.52, \\ 8.33(\eta_r - 0.40) & ; \text{for } 0.40 \le \eta_r \le 0.52, \\ 0 & ; \text{for } \eta_r < 0.40. \end{cases}$$

$$\eta_r = \eta_0 / \eta_{sat}, \eta_{sat} = 0.482, \eta_{wilt} = 0.286,$$

$$a_s = 0.002, b_s = 0.003, \rho_s^{dry} = 1600, c_s^{dry} = 890, a_n = 0.083, b_n = 12.$$

Vegetation parameterisation

The vegetation temperature T_f is calculated from a surface energy balance

$$0 = R_{sw}^{in}(1 - \alpha_f) + R_{lw}^{in} - \sigma_{SR}T_f^4 \cos \alpha - H_f - \lambda E_f$$

using Newton iteration, where the outward long-wave radiation and sensible (H_f) and latent (E_f) heat fluxes are treated as functions of T_f , with

$$H_f = \rho c_p (\theta_f - \theta_1) / r_H,$$

$$E_f = (1 - \beta) E_{tr} + \beta E_w,$$

$$E_{tr} = \rho(q_f^* - q_1)/(r_H + r_s),$$

$$E_w = \rho (q_f^* - q_1) / r_H,$$

$$\beta = \begin{cases} 1; & \text{if condensation } (q_1 > q_f^*) \\ m_r / (0.0002LAI); & \text{if evapotranspiration} \end{cases}$$

$$\frac{\partial m_r}{\partial t} = P - P_g - \beta E_w / \rho_w,$$

where m_r is the moisture reservoir and r_H is the aerodynamic resistance (see Section 2.6.4).

The vegetation specific humidity q_f is calculated from $q_f = q_f^* - E_f r_S / \rho$, and the stomatal resistance r_S is calculated using

$$r_S = \frac{r_{si}}{IAI} F_1 F_2^{-1} F_3^{-1} F_4^{-1}$$

and

$$F_1 = \frac{1+f}{f + (r_{si}/5000)}, \quad F_2 = \frac{\eta_d - \eta_{wilt}}{0.75\eta_{sat} - \eta_{wilt}},$$

$$F_3 = 1 - 0.00025(e_f^* - e_1), \quad F_4 = 1 - 0.0016(298 - T_1)^2, \quad f = 0.55 \frac{R_{sw}^{in}}{R^*} \frac{2}{LAI}.$$

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Table A.1: Vegetation (land-use) characteristics used in TAPM.

-1: Permanent snow/ice	Table A.1: Vegetation (land-use) characteristics	used in TA	APM.		1
0: Water -<	Vegetation Types:	$h_f(\mathbf{m})$	$oldsymbol{\sigma}_f$	LAI	r_{si} (m ⁻¹)
1: Forest – tall mid-dense 42.00 0.75 4.8 370 2: Forest – tall mid-dense 36.50 0.75 6.3 330 3: Forest – dense 25.00 0.75 5.0 260 4: Forest – mid-dense 17.00 0.50 3.8 200 5: Forest – sparse (woodland) 12.00 0.25 2.8 150 6: Forest – very sparse (woodland) 10.00 0.25 2.5 130 7: Forest – low dense 9.00 0.75 3.9 200 8: Forest – low mid-dense 7.00 0.50 2.8 150 9: Forest – low sparse (woodland) 5.50 0.25 2.0 110 10: Shrub-land – tall mid-dense (scrub) 3.00 0.50 2.8 150 9: Forest – low sparse (woodland) 3.00 0.50 2.5 1.0 110 10: Shrub-land – tall mid-dense (scrub) 3.00 0.50 2.6 160 11: Shrub-land – tall wery sparse 2.00 0.25 1.7 100 12: Shrub-land – low	-1: Permanent snow/ice	-	-	1	-
2: Forest – tall mid-dense 36.50 0.75 6.3 330 3: Forest – dense 25.00 0.75 5.0 260 4: Forest – mid-dense 17.00 0.50 3.8 200 5: Forest – sparse (woodland) 12.00 0.25 2.8 150 6: Forest – low dense 9.00 0.75 3.9 200 8: Forest – low dense 9.00 0.75 3.9 200 8: Forest – low mid-dense 7.00 0.50 2.8 150 9: Forest – low sparse (woodland) 5.50 0.25 2.0 110 10: Shrub-land – tall mid-dense (scrub) 3.00 0.50 2.8 150 9: Forest – low sparse (woodland) 5.50 0.25 2.0 110 10: Shrub-land – tall mid-dense (scrub) 3.00 0.50 2.8 150 9: Forest – low sparse 2.50 0.25 1.7 100 12: Shrub-land – tall sparse 2.50 0.25 1.7 100 12: Shrub-land – tall sparse 0.60 <t< td=""><td>0: Water</td><td>-</td><td>-</td><td>-</td><td>-</td></t<>	0: Water	-	-	-	-
3: Forest – dense 25.00 0.75 5.0 260 4: Forest – mid-dense 17.00 0.50 3.8 200 5: Forest – sparse (woodland) 12.00 0.25 2.8 150 6: Forest – very sparse (woodland) 10.00 0.25 2.5 130 7: Forest – low dense 9.00 0.75 3.9 200 8: Forest – low mid-dense 7.00 0.50 2.8 150 9: Forest – low sparse (woodland) 5.50 0.25 2.0 110 10: Shrub-land – tall mid-dense (scrub) 3.00 0.50 2.6 160 11: Shrub-land – tall sparse 2.50 0.25 1.7 100 12: Shrub-land – tow garse 2.00 0.25 1.7 100 14: Shrub-land – low sparse 0.60 0.25 1.5 90 15: Shrub-land – low very sparse 0.50 0.25 1.5 90 15: Shrub-land – low very sparse 0.50 0.25 1.2 80 16: Grassland – sparse hummock 0.50	1: Forest – tall dense	42.00	0.75	4.8	370
4: Forest – mid-dense 17.00 0.50 3.8 200 5: Forest – sparse (woodland) 12.00 0.25 2.8 150 6: Forest – very sparse (woodland) 10.00 0.25 2.5 130 7: Forest – low dense 9.00 0.75 3.9 200 8: Forest – low mid-dense 7.00 0.50 2.8 150 9: Forest – low sparse (woodland) 5.50 0.25 2.0 110 10: Shrub-land – tall mid-dense (scrub) 3.00 0.50 2.6 160 11: Shrub-land – tall sparse 2.50 0.25 1.7 100 12: Shrub-land – tall very sparse 2.00 0.25 1.9 120 13: Shrub-land – low mid-dense 1.00 0.50 1.4 90 14: Shrub-land – low wird-dense 1.00 0.50 1.4 90 14: Shrub-land – low very sparse 0.50 0.25 1.5 90 15: Shrub-land – low very sparse 0.50 0.25 1.2 80 16: Grassland – sparse hummock	2: Forest – tall mid-dense	36.50	0.75	6.3	330
5: Forest – sparse (woodland) 12.00 0.25 2.8 150 6: Forest – very sparse (woodland) 10.00 0.25 2.5 130 7: Forest – low dense 9.00 0.75 3.9 200 8: Forest – low mid-dense 7.00 0.50 2.8 150 9: Forest – low sparse (woodland) 5.50 0.25 2.0 110 10: Shrub-land – tall mid-dense (scrub) 3.00 0.50 2.6 160 11: Shrub-land – tall sparse 2.50 0.25 1.7 100 12: Shrub-land – tow mid-dense 1.00 0.50 1.4 90 13: Shrub-land – low mid-dense 1.00 0.50 1.4 90 14: Shrub-land – low very sparse 0.60 0.25 1.5 90 15: Shrub-land – low very sparse 0.50 0.25 1.2 80 15: Shrub-land – low very sparse 0.50 0.25 1.2 80 15: Shrub-land – low very sparse 0.50 0.25 1.2 80 15: Grassland – sparse hummock<	3: Forest – dense	25.00	0.75	5.0	260
6: Forest – very sparse (woodland) 10.00 0.25 2.5 130 7: Forest – low dense 9.00 0.75 3.9 200 8: Forest – low mid-dense 7.00 0.50 2.8 150 9: Forest – low sparse (woodland) 5.50 0.25 2.0 110 10: Shrub-land – tall mid-dense (scrub) 3.00 0.50 2.6 160 11: Shrub-land – tall sparse 2.50 0.25 1.7 100 12: Shrub-land – tall very sparse 2.00 0.25 1.9 120 13: Shrub-land – low mid-dense 1.00 0.50 1.4 90 14: Shrub-land – low very sparse 0.60 0.25 1.5 90 15: Shrub-land – low very sparse 0.50 0.25 1.2 80 16: Grassland – low very sparse 0.50 0.25 1.2 80 16: Grassland – sparse hummock 0.45 0.25 1.4 90 18: Grassland – wery sparse hummock 0.45 0.25 1.4 90 19: Grassland – sparse tus	4: Forest – mid-dense	17.00	0.50	3.8	200
7: Forest – low dense 9.00 0.75 3.9 200 8: Forest – low mid-dense 7.00 0.50 2.8 150 9: Forest – low sparse (woodland) 5.50 0.25 2.0 110 10: Shrub-land – tall mid-dense (scrub) 3.00 0.50 2.6 160 11: Shrub-land – tall very sparse 2.50 0.25 1.7 100 12: Shrub-land – low mid-dense 1.00 0.50 1.4 90 13: Shrub-land – low mid-dense 1.00 0.50 1.4 90 14: Shrub-land – low sparse 0.60 0.25 1.5 90 15: Shrub-land – low very sparse 0.50 0.25 1.5 90 15: Shrub-land – low very sparse 0.50 0.25 1.5 90 15: Shrub-land – low very sparse 0.50 0.25 1.2 80 16: Grassland – sparse hummock 0.50 0.25 1.2 80 17: Grassland – sparse hummock 0.45 0.25 1.4 90 18: Grassland – sparse tussock	5: Forest – sparse (woodland)	12.00	0.25	2.8	150
8: Forest – low mid-dense 7.00 0.50 2.8 150 9: Forest – low sparse (woodland) 5.50 0.25 2.0 110 10: Shrub-land – tall mid-dense (scrub) 3.00 0.50 2.6 160 11: Shrub-land – tall sparse 2.50 0.25 1.7 100 12: Shrub-land – tall very sparse 2.00 0.25 1.9 120 13: Shrub-land – low mid-dense 1.00 0.50 1.4 90 14: Shrub-land – low very sparse 0.60 0.25 1.5 90 15: Shrub-land – low very sparse 0.60 0.25 1.5 90 15: Shrub-land – low very sparse 0.50 0.25 1.2 80 16: Grassland – low very sparse 0.50 0.25 1.2 80 16: Grassland – sparse hummock 0.45 0.25 1.4 90 18: Grassland – very sparse hummock 0.45 0.25 1.4 90 18: Grassland – sparse tussock 0.40 0.50 1.2 80 20: Grassland – sparse	6: Forest – very sparse (woodland)	10.00	0.25	2.5	130
9: Forest – low sparse (woodland) 5.50 0.25 2.0 110 10: Shrub-land – tall mid-dense (scrub) 3.00 0.50 2.6 160 11: Shrub-land – tall sparse 2.50 0.25 1.7 100 12: Shrub-land – tall very sparse 2.00 0.25 1.9 120 13: Shrub-land – low mid-dense 1.00 0.50 1.4 90 14: Shrub-land – low sparse 0.60 0.25 1.5 90 15: Shrub-land – low very sparse 0.50 0.25 1.2 80 16: Grassland – low very sparse 0.50 0.25 1.2 80 16: Grassland – sparse hummock 0.50 0.25 1.6 90 17: Grassland – very sparse hummock 0.45 0.25 1.4 90 18: Grassland – dense tussock 0.75 0.75 2.3 150 19: Grassland – sparse tussock 0.60 0.50 1.2 80 20: Grassland – sparse tussock 0.45 0.25 1.7 100 21: Grassland – sparse t	7: Forest – low dense	9.00	0.75	3.9	200
10: Shrub-land – tall mid-dense (scrub) 3.00 0.50 2.6 160 11: Shrub-land – tall sparse 2.50 0.25 1.7 100 12: Shrub-land – tall very sparse 2.00 0.25 1.9 120 13: Shrub-land – low mid-dense 1.00 0.50 1.4 90 14: Shrub-land – low sparse 0.60 0.25 1.5 90 15: Shrub-land – low very sparse 0.50 0.25 1.2 80 16: Grassland – sparse hummock 0.50 0.25 1.6 90 17: Grassland – sparse hummock 0.45 0.25 1.4 90 18: Grassland – sparse hummock 0.45 0.25 1.4 90 18: Grassland – sparse hummock 0.45 0.25 1.4 90 18: Grassland – sparse hummock 0.45 0.25 1.4 90 18: Grassland – sparse tussock 0.60 0.50 1.2 80 20: Grassland – sparse tussock 0.45 0.25 1.7 100 21: Grassland – very sparse tussoc	8: Forest – low mid-dense	7.00	0.50	2.8	150
11: Shrub-land – tall sparse 2.50 0.25 1.7 100 12: Shrub-land – tall very sparse 2.00 0.25 1.9 120 13: Shrub-land – low mid-dense 1.00 0.50 1.4 90 14: Shrub-land – low sparse 0.60 0.25 1.5 90 15: Shrub-land – low very sparse 0.50 0.25 1.2 80 16: Grassland – sparse hummock 0.50 0.25 1.6 90 17: Grassland – sparse hummock 0.45 0.25 1.4 90 18: Grassland – very sparse hummock 0.45 0.25 1.4 90 18: Grassland – sparse hummock 0.75 0.75 2.3 150 19: Grassland – sparse hummock 0.60 0.50 1.2 80 20: Grassland – sparse tussock 0.45 0.25 1.7 100 21: Grassland – sparse tussock 0.40 0.25 1.2 80 22: Pasture/herb-field – dense (perennial) 0.60 0.75 2.3 80 23: Pasture/herb-field – dense (seasonal) 0.60 0.75 2.3 80	9: Forest – low sparse (woodland)	5.50	0.25	2.0	110
12: Shrub-land - tall very sparse 2.00 0.25 1.9 120 13: Shrub-land - low mid-dense 1.00 0.50 1.4 90 14: Shrub-land - low sparse 0.60 0.25 1.5 90 15: Shrub-land - low very sparse 0.50 0.25 1.2 80 16: Grassland - sparse hummock 0.50 0.25 1.6 90 17: Grassland - very sparse hummock 0.45 0.25 1.4 90 18: Grassland - dense tussock 0.75 0.75 2.3 150 19: Grassland - mid-dense tussock 0.60 0.50 1.2 80 20: Grassland - sparse tussock 0.45 0.25 1.7 100 21: Grassland - very sparse tussock 0.40 0.25 1.2 80 22: Pasture/herb-field - dense (perennial) 0.60 0.75 2.3 80 23: Pasture/herb-field - dense (seasonal) 0.60 0.75 2.3 80 24: Pasture/herb-field - mid-dense (perennial) 0.45 0.50 1.2 40 25: Pasture/herb-field - mid-dense (seasonal) 0.45 0.50 1.2 40 26: Pasture/herb-field - sparse 0.35 0.25 1.9 120 27: Pasture/herb-field - very sparse 0.30 0.25 1.0 80 28: Littoral 2.50 0.50 3.0 180 29: Permanent lake	10: Shrub-land – tall mid-dense (scrub)	3.00	0.50	2.6	160
13: Shrub-land – low mid-dense 1.00 0.50 1.4 90 14: Shrub-land – low sparse 0.60 0.25 1.5 90 15: Shrub-land – low very sparse 0.50 0.25 1.2 80 16: Grassland – sparse hummock 0.50 0.25 1.6 90 17: Grassland – very sparse hummock 0.45 0.25 1.4 90 18: Grassland – dense tussock 0.75 0.75 2.3 150 19: Grassland – mid-dense tussock 0.60 0.50 1.2 80 20: Grassland – sparse tussock 0.45 0.25 1.7 100 21: Grassland – very sparse tussock 0.40 0.25 1.2 80 22: Pasture/herb-field – dense (perennial) 0.60 0.75 2.3 80 23: Pasture/herb-field – dense (seasonal) 0.60 0.75 2.3 80 24: Pasture/herb-field – mid-dense (perennial) 0.45 0.50 1.2 40 25: Pasture/herb-field – sparse 0.35 0.25 1.9 120 27: Pasture/herb-field – very sparse 0.30 0.25 1.0 80 </td <td>11: Shrub-land – tall sparse</td> <td>2.50</td> <td>0.25</td> <td>1.7</td> <td>100</td>	11: Shrub-land – tall sparse	2.50	0.25	1.7	100
14: Shrub-land – low sparse 0.60 0.25 1.5 90 15: Shrub-land – low very sparse 0.50 0.25 1.2 80 16: Grassland – sparse hummock 0.50 0.25 1.6 90 17: Grassland – very sparse hummock 0.45 0.25 1.4 90 18: Grassland – dense tussock 0.75 0.75 2.3 150 19: Grassland – mid-dense tussock 0.60 0.50 1.2 80 20: Grassland – sparse tussock 0.45 0.25 1.7 100 21: Grassland – very sparse tussock 0.40 0.25 1.2 80 22: Pasture/herb-field – dense (perennial) 0.60 0.75 2.3 80 22: Pasture/herb-field – dense (seasonal) 0.60 0.75 2.3 80 24: Pasture/herb-field – mid-dense (perennial) 0.45 0.50 1.2 40 25: Pasture/herb-field – mid-dense (seasonal) 0.45 0.50 1.2 40 26: Pasture/herb-field – very sparse 0.35 0.25 1.9 120 27: Pasture/herb-field – very sparse 0.30 0.25 1.0	12: Shrub-land – tall very sparse	2.00	0.25	1.9	120
15: Shrub-land – low very sparse 0.50 0.25 1.2 80 16: Grassland – sparse hummock 0.50 0.25 1.6 90 17: Grassland – very sparse hummock 0.45 0.25 1.4 90 18: Grassland – dense tussock 0.75 0.75 2.3 150 19: Grassland – mid-dense tussock 0.60 0.50 1.2 80 20: Grassland – sparse tussock 0.45 0.25 1.7 100 21: Grassland – very sparse tussock 0.40 0.25 1.2 80 22: Pasture/herb-field – dense (perennial) 0.60 0.75 2.3 80 23: Pasture/herb-field – dense (seasonal) 0.60 0.75 2.3 80 24: Pasture/herb-field – mid-dense (perennial) 0.45 0.50 1.2 40 25: Pasture/herb-field – mid-dense (seasonal) 0.45 0.50 1.2 40 26: Pasture/herb-field – very sparse 0.35 0.25 1.9 120 27: Pasture/herb-field – very sparse 0.30 0.25 1.0 80<	13: Shrub-land – low mid-dense	1.00	0.50	1.4	90
16: Grassland – sparse hummock 0.50 0.25 1.6 90 17: Grassland – very sparse hummock 0.45 0.25 1.4 90 18: Grassland – dense tussock 0.75 0.75 2.3 150 19: Grassland – mid-dense tussock 0.60 0.50 1.2 80 20: Grassland – sparse tussock 0.45 0.25 1.7 100 21: Grassland – very sparse tussock 0.40 0.25 1.2 80 22: Pasture/herb-field – dense (perennial) 0.60 0.75 2.3 80 23: Pasture/herb-field – dense (seasonal) 0.60 0.75 2.3 80 24: Pasture/herb-field – mid-dense (perennial) 0.45 0.50 1.2 40 25: Pasture/herb-field – mid-dense (seasonal) 0.45 0.50 1.2 40 26: Pasture/herb-field – very sparse 0.30 0.25 1.9 120 27: Pasture/herb-field – very sparse 0.30 0.25 1.0 80 28: Littoral 2.50 0.50 3.0 180	14: Shrub-land – low sparse	0.60	0.25	1.5	90
17: Grassland – very sparse hummock 0.45 0.25 1.4 90 18: Grassland – dense tussock 0.75 0.75 2.3 150 19: Grassland – mid-dense tussock 0.60 0.50 1.2 80 20: Grassland – sparse tussock 0.45 0.25 1.7 100 21: Grassland – very sparse tussock 0.40 0.25 1.2 80 22: Pasture/herb-field – dense (perennial) 0.60 0.75 2.3 80 23: Pasture/herb-field – dense (seasonal) 0.60 0.75 2.3 80 24: Pasture/herb-field – mid-dense (seasonal) 0.45 0.50 1.2 40 25: Pasture/herb-field – mid-dense (seasonal) 0.45 0.50 1.2 40 26: Pasture/herb-field – sparse 0.35 0.25 1.9 120 27: Pasture/herb-field – very sparse 0.30 0.25 1.0 80 28: Littoral 2.50 0.50 3.0 180 29: Permanent lake - - - - 30: Ephemeral lake (salt) - - - - 31:	15: Shrub-land – low very sparse	0.50	0.25	1.2	80
17: Grassland – very sparse hummock 0.45 0.25 1.4 90 18: Grassland – dense tussock 0.75 0.75 2.3 150 19: Grassland – mid-dense tussock 0.60 0.50 1.2 80 20: Grassland – sparse tussock 0.45 0.25 1.7 100 21: Grassland – very sparse tussock 0.40 0.25 1.2 80 22: Pasture/herb-field – dense (perennial) 0.60 0.75 2.3 80 23: Pasture/herb-field – dense (seasonal) 0.60 0.75 2.3 80 24: Pasture/herb-field – mid-dense (seasonal) 0.45 0.50 1.2 40 25: Pasture/herb-field – mid-dense (seasonal) 0.45 0.50 1.2 40 26: Pasture/herb-field – sparse 0.35 0.25 1.9 120 27: Pasture/herb-field – very sparse 0.30 0.25 1.0 80 28: Littoral 2.50 0.50 3.0 180 29: Permanent lake - - - - 30: Ephemeral lake (salt) - - - - 31:	16: Grassland – sparse hummock	0.50	0.25	1.6	90
19: Grassland – mid-dense tussock 0.60 0.50 1.2 80 20: Grassland – sparse tussock 0.45 0.25 1.7 100 21: Grassland – very sparse tussock 0.40 0.25 1.2 80 22: Pasture/herb-field – dense (perennial) 0.60 0.75 2.3 80 23: Pasture/herb-field – dense (seasonal) 0.60 0.75 2.3 80 24: Pasture/herb-field – mid-dense (seasonal) 0.45 0.50 1.2 40 25: Pasture/herb-field – mid-dense (seasonal) 0.45 0.50 1.2 40 26: Pasture/herb-field – sparse 0.35 0.25 1.9 120 27: Pasture/herb-field – very sparse 0.30 0.25 1.0 80 28: Littoral 2.50 0.50 3.0 180 29: Permanent lake - - - 30: Ephemeral lake (salt) - - - 31: Urban (low) 8.00 0.75 2.0 100 32: Urban (medium) 12.00 0.75 2.0 100 35: Urban (cbd) 20.00 0.75	-	0.45	0.25	1.4	90
20: Grassland – sparse tussock 0.45 0.25 1.7 100 21: Grassland – very sparse tussock 0.40 0.25 1.2 80 22: Pasture/herb-field – dense (perennial) 0.60 0.75 2.3 80 23: Pasture/herb-field – dense (seasonal) 0.60 0.75 2.3 80 24: Pasture/herb-field – dense (seasonal) 0.60 0.75 2.3 80 24: Pasture/herb-field – mid-dense (perennial) 0.45 0.50 1.2 40 25: Pasture/herb-field – mid-dense (seasonal) 0.45 0.50 1.2 40 26: Pasture/herb-field – sparse 0.35 0.25 1.9 120 27: Pasture/herb-field – very sparse 0.30 0.25 1.0 80 28: Littoral 2.50 0.50 3.0 180 29: Permanent lake - - - - 30: Ephemeral lake (salt) - - - 31: Urban (low) 8.00 0.75 2.0 100 32: Urban (medium) 12.00 0.75 2.0 100 35: Urban (cbd) 20.00	18: Grassland – dense tussock	0.75	0.75	2.3	150
21: Grassland – very sparse tussock 0.40 0.25 1.2 80 22: Pasture/herb-field – dense (perennial) 0.60 0.75 2.3 80 23: Pasture/herb-field – dense (seasonal) 0.60 0.75 2.3 80 24: Pasture/herb-field – dense (seasonal) 0.45 0.50 1.2 40 25: Pasture/herb-field – mid-dense (seasonal) 0.45 0.50 1.2 40 26: Pasture/herb-field – sparse 0.35 0.25 1.9 120 27: Pasture/herb-field – very sparse 0.30 0.25 1.0 80 28: Littoral 2.50 0.50 3.0 180 29: Permanent lake - - - - 30: Ephemeral lake (salt) - - - - 31: Urban (low) 8.00 0.75 2.0 100 32: Urban (medium) 12.00 0.75 2.0 100 34: Urban (high) 16.00 0.75 2.0 100 35: Urban (cbd) 20.00 0.75 2.0 100 36: Industrial (medium) 10.00 0.75 </td <td>19: Grassland – mid-dense tussock</td> <td>0.60</td> <td>0.50</td> <td>1.2</td> <td>80</td>	19: Grassland – mid-dense tussock	0.60	0.50	1.2	80
22: Pasture/herb-field – dense (perennial) 0.60 0.75 2.3 80 23: Pasture/herb-field – dense (seasonal) 0.60 0.75 2.3 80 24: Pasture/herb-field – mid-dense (perennial) 0.45 0.50 1.2 40 25: Pasture/herb-field – mid-dense (seasonal) 0.45 0.50 1.2 40 26: Pasture/herb-field – sparse 0.35 0.25 1.9 120 27: Pasture/herb-field – very sparse 0.30 0.25 1.0 80 28: Littoral 2.50 0.50 3.0 180 29: Permanent lake - - - - 30: Ephemeral lake (salt) - - - - 31: Urban 10.00 0.75 2.0 100 32: Urban (low) 8.00 0.75 2.0 100 34: Urban (high) 16.00 0.75 2.0 100 35: Urban (cbd) 20.00 0.75 2.0 100 36: Industrial (low) 10.00 0.75 2.0 100 37: Industrial (medium) 10.00 0.75 2.0	20: Grassland – sparse tussock	0.45	0.25	1.7	100
23: Pasture/herb-field – dense (seasonal) 0.60 0.75 2.3 80 24: Pasture/herb-field – mid-dense (perennial) 0.45 0.50 1.2 40 25: Pasture/herb-field – mid-dense (seasonal) 0.45 0.50 1.2 40 26: Pasture/herb-field – sparse 0.35 0.25 1.9 120 27: Pasture/herb-field – very sparse 0.30 0.25 1.0 80 28: Littoral 2.50 0.50 3.0 180 29: Permanent lake - - - - 30: Ephemeral lake (salt) - - - - 31: Urban 10.00 0.75 2.0 100 32: Urban (low) 8.00 0.75 2.0 100 33: Urban (medium) 12.00 0.75 2.0 100 34: Urban (high) 16.00 0.75 2.0 100 35: Urban (cbd) 20.00 0.75 2.0 100 36: Industrial (low) 10.00 0.75 2.0 100 37: Industrial (medium) 10.00 0.75 2.0 100 <td>21: Grassland – very sparse tussock</td> <td>0.40</td> <td>0.25</td> <td>1.2</td> <td>80</td>	21: Grassland – very sparse tussock	0.40	0.25	1.2	80
24: Pasture/herb-field – mid-dense (perennial) 0.45 0.50 1.2 40 25: Pasture/herb-field – mid-dense (seasonal) 0.45 0.50 1.2 40 26: Pasture/herb-field – sparse 0.35 0.25 1.9 120 27: Pasture/herb-field – very sparse 0.30 0.25 1.0 80 28: Littoral 2.50 0.50 3.0 180 29: Permanent lake - - - - 30: Ephemeral lake (salt) - - - - 31: Urban 10.00 0.75 2.0 100 32: Urban (low) 8.00 0.75 2.0 100 33: Urban (medium) 12.00 0.75 2.0 100 34: Urban (high) 16.00 0.75 2.0 100 35: Urban (cbd) 20.00 0.75 2.0 100 36: Industrial (low) 10.00 0.75 2.0 100 37: Industrial (medium) 10.00 0.75 2.0 100	22: Pasture/herb-field – dense (perennial)	0.60	0.75	2.3	80
25: Pasture/herb-field – mid-dense (seasonal) 0.45 0.50 1.2 40 26: Pasture/herb-field – sparse 0.35 0.25 1.9 120 27: Pasture/herb-field – very sparse 0.30 0.25 1.0 80 28: Littoral 2.50 0.50 3.0 180 29: Permanent lake - - - - 30: Ephemeral lake (salt) - - - - 31: Urban 10.00 0.75 2.0 100 32: Urban (low) 8.00 0.75 2.0 100 33: Urban (medium) 12.00 0.75 2.0 100 34: Urban (high) 16.00 0.75 2.0 100 35: Urban (cbd) 20.00 0.75 2.0 100 36: Industrial (low) 10.00 0.75 2.0 100 37: Industrial (medium) 10.00 0.75 2.0 100	23: Pasture/herb-field – dense (seasonal)	0.60	0.75	2.3	80
26: Pasture/herb-field – sparse 0.35 0.25 1.9 120 27: Pasture/herb-field – very sparse 0.30 0.25 1.0 80 28: Littoral 2.50 0.50 3.0 180 29: Permanent lake - - - - 30: Ephemeral lake (salt) - - - - 31: Urban 10.00 0.75 2.0 100 32: Urban (low) 8.00 0.75 2.0 100 33: Urban (medium) 12.00 0.75 2.0 100 34: Urban (high) 16.00 0.75 2.0 100 35: Urban (cbd) 20.00 0.75 2.0 100 36: Industrial (low) 10.00 0.75 2.0 100 37: Industrial (medium) 10.00 0.75 2.0 100	24: Pasture/herb-field – mid-dense (perennial)	0.45	0.50	1.2	40
27: Pasture/herb-field – very sparse 0.30 0.25 1.0 80 28: Littoral 2.50 0.50 3.0 180 29: Permanent lake - - - - 30: Ephemeral lake (salt) - - - - 31: Urban 10.00 0.75 2.0 100 32: Urban (low) 8.00 0.75 2.0 100 33: Urban (medium) 12.00 0.75 2.0 100 34: Urban (high) 16.00 0.75 2.0 100 35: Urban (cbd) 20.00 0.75 2.0 100 36: Industrial (low) 10.00 0.75 2.0 100 37: Industrial (medium) 10.00 0.75 2.0 100	25: Pasture/herb-field – mid-dense (seasonal)	0.45	0.50	1.2	40
28: Littoral 2.50 0.50 3.0 180 29: Permanent lake - - - - 30: Ephemeral lake (salt) - - - - 31: Urban 10.00 0.75 2.0 100 32: Urban (low) 8.00 0.75 2.0 100 33: Urban (medium) 12.00 0.75 2.0 100 34: Urban (high) 16.00 0.75 2.0 100 35: Urban (cbd) 20.00 0.75 2.0 100 36: Industrial (low) 10.00 0.75 2.0 100 37: Industrial (medium) 10.00 0.75 2.0 100	26: Pasture/herb-field – sparse	0.35	0.25	1.9	120
29: Permanent lake - - - - 30: Ephemeral lake (salt) - - - - 31: Urban 10.00 0.75 2.0 100 32: Urban (low) 8.00 0.75 2.0 100 33: Urban (medium) 12.00 0.75 2.0 100 34: Urban (high) 16.00 0.75 2.0 100 35: Urban (cbd) 20.00 0.75 2.0 100 36: Industrial (low) 10.00 0.75 2.0 100 37: Industrial (medium) 10.00 0.75 2.0 100	27: Pasture/herb-field – very sparse	0.30	0.25	1.0	80
30: Ephemeral lake (salt) - - - - 31: Urban 10.00 0.75 2.0 100 32: Urban (low) 8.00 0.75 2.0 100 33: Urban (medium) 12.00 0.75 2.0 100 34: Urban (high) 16.00 0.75 2.0 100 35: Urban (cbd) 20.00 0.75 2.0 100 36: Industrial (low) 10.00 0.75 2.0 100 37: Industrial (medium) 10.00 0.75 2.0 100	28: Littoral	2.50	0.50	3.0	180
31: Urban 10.00 0.75 2.0 100 32: Urban (low) 8.00 0.75 2.0 100 33: Urban (medium) 12.00 0.75 2.0 100 34: Urban (high) 16.00 0.75 2.0 100 35: Urban (cbd) 20.00 0.75 2.0 100 36: Industrial (low) 10.00 0.75 2.0 100 37: Industrial (medium) 10.00 0.75 2.0 100	29: Permanent lake	-	-	-	-
32: Urban (low) 8.00 0.75 2.0 100 33: Urban (medium) 12.00 0.75 2.0 100 34: Urban (high) 16.00 0.75 2.0 100 35: Urban (cbd) 20.00 0.75 2.0 100 36: Industrial (low) 10.00 0.75 2.0 100 37: Industrial (medium) 10.00 0.75 2.0 100	30: Ephemeral lake (salt)	-	-	-	_
33: Urban (medium) 12.00 0.75 2.0 100 34: Urban (high) 16.00 0.75 2.0 100 35: Urban (cbd) 20.00 0.75 2.0 100 36: Industrial (low) 10.00 0.75 2.0 100 37: Industrial (medium) 10.00 0.75 2.0 100	31: Urban	10.00	0.75	2.0	100
33: Urban (medium) 12.00 0.75 2.0 100 34: Urban (high) 16.00 0.75 2.0 100 35: Urban (cbd) 20.00 0.75 2.0 100 36: Industrial (low) 10.00 0.75 2.0 100 37: Industrial (medium) 10.00 0.75 2.0 100	32: Urban (low)	8.00	0.75	2.0	100
34: Urban (high) 16.00 0.75 2.0 100 35: Urban (cbd) 20.00 0.75 2.0 100 36: Industrial (low) 10.00 0.75 2.0 100 37: Industrial (medium) 10.00 0.75 2.0 100	` /	12.00	0.75	2.0	100
35: Urban (cbd) 20.00 0.75 2.0 100 36: Industrial (low) 10.00 0.75 2.0 100 37: Industrial (medium) 10.00 0.75 2.0 100	,				
36: Industrial (low) 10.00 0.75 2.0 100 37: Industrial (medium) 10.00 0.75 2.0 100	`	1			1
37: Industrial (medium) 10.00 0.75 2.0 100	` ′				100
			0.75		1
\ \(\(\(\) \\ \) \\ \ \ \ \ \ \ \ \ \	38: Industrial (high)	10.00	0.75	2.0	100

Other variables are

 α_f = Vegetation albedo (0.2),

 q_f^* = Vegetation saturated specific humidity,

 e_f^* = Vegetation saturated vapour pressure,

$$R^* = \begin{cases} 30 \text{ W m}^{-2}; & \text{if } z_{0f} > 0.3\\ 100 \text{ W m}^{-2}; & \text{if } z_{0f} \le 0.3 \end{cases}$$

 z_{0f} = vegetation roughness length (m) = 0.1 + h_f /10 ($z_{0f} \le 2.0$ m),

 h_f = vegetation height (m),

 σ_f = fraction of surface covered by vegetation,

LAI = Leaf Area Index,

 r_{si} = minimum stomatal resistance (s⁻¹).

The vegetation (land-use) types used in TAPM are based on a CSIRO Wildlife and Ecology Categorisation (Graetz, 1998, personal communication), and are listed in Table A.1, with urban/industrial conditions modified as described in Section 2.6.3.

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